

STANFORD SYNCHROTRON RADIATION LABORATORY

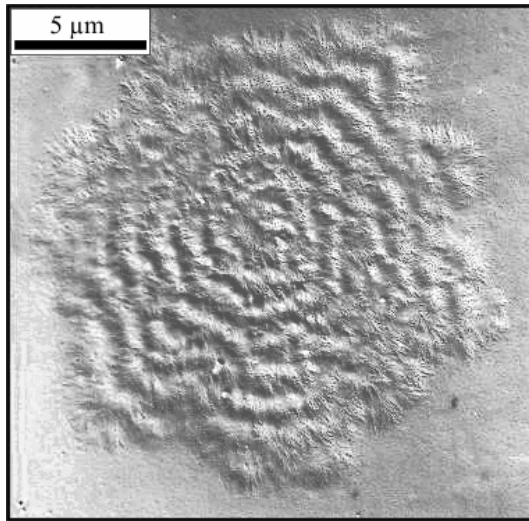


# *Everything You Ever Wanted to Know About SAXS But Were Afraid to Ask*

**John A Pople**

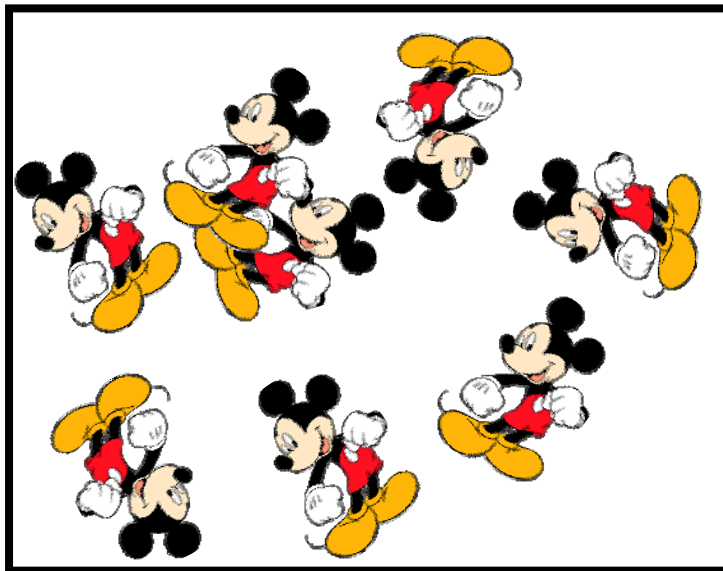
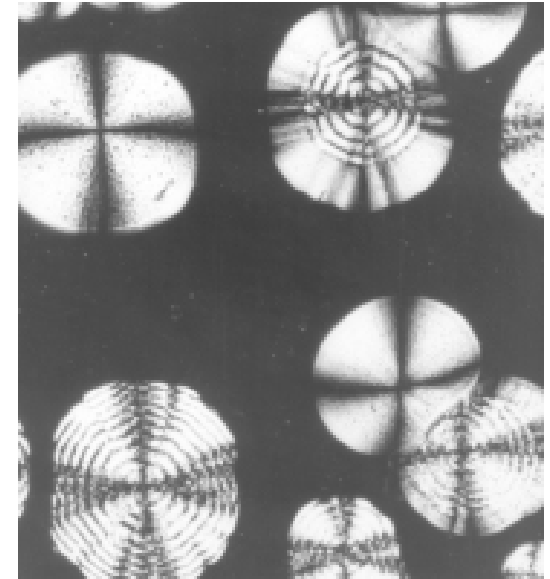
*Stanford Synchrotron Radiation Laboratory,  
Stanford Linear Accelerator Center, Stanford CA 94309*

# Scattering or Microscopy?



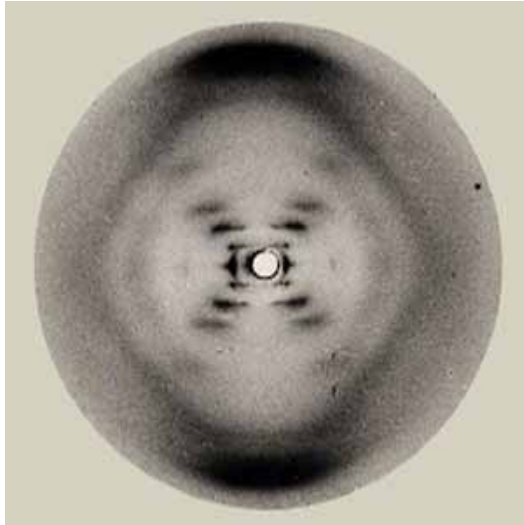
## *Microscopy good for:*

- Local detail
- Surface detail
- Faithfully represents local complexities



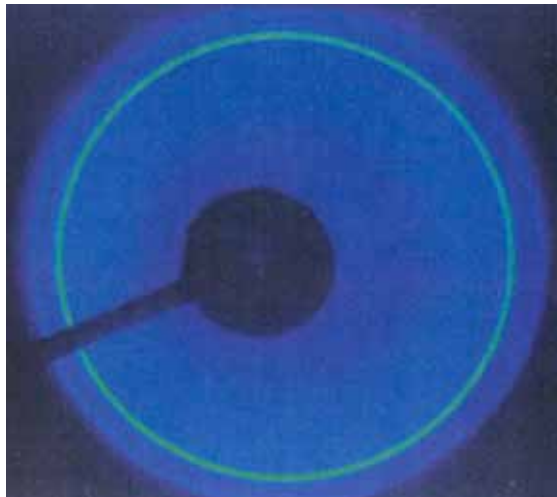
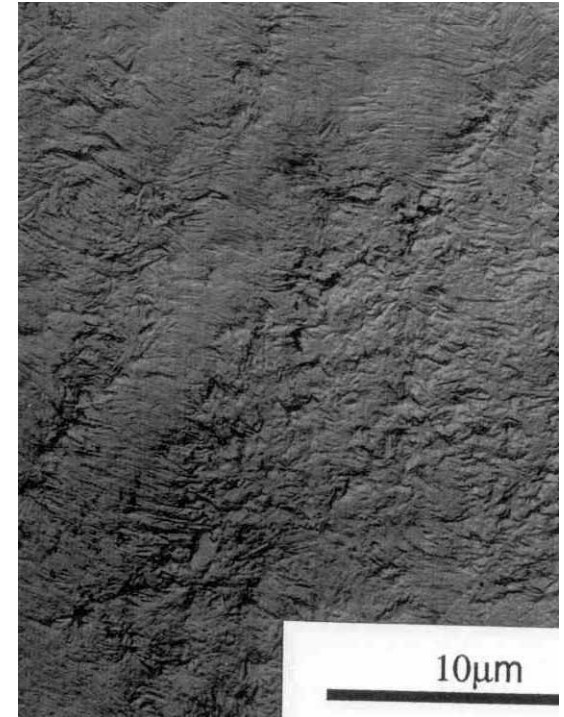
E.g. if objective is to monitor the degree to which Mickey's nose(s) and ears hold to a circular micromorphology... use microscopy not scattering

# Scattering or Microscopy?

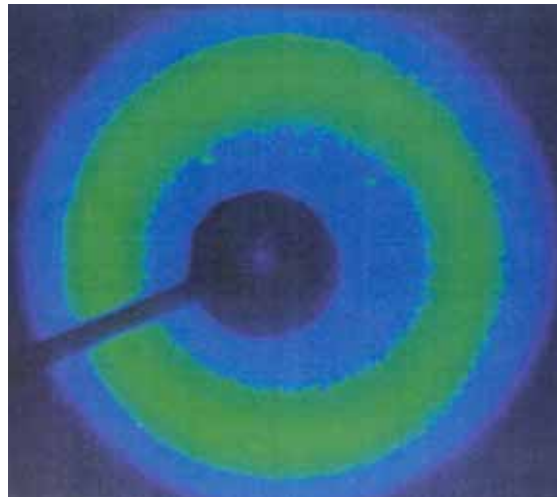


## Scattering good for:

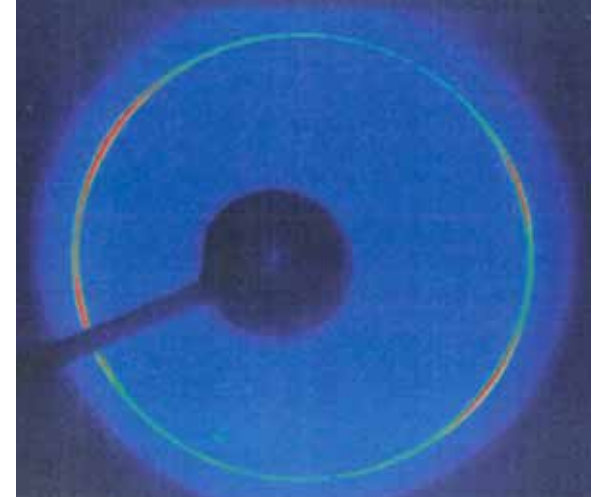
- Global parameters, distributions; 1<sup>st</sup> order
- Different sample states
- Non destructive sample preparation
- In-situ transitional studies



Solid

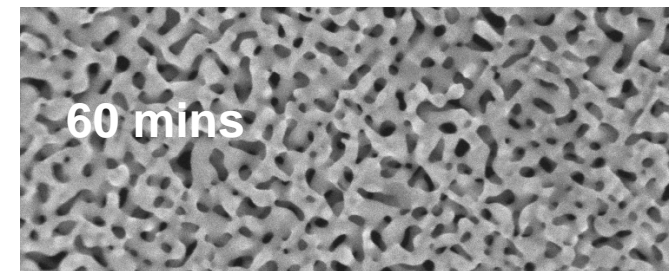
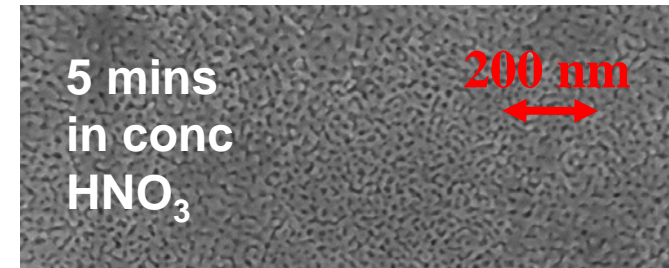
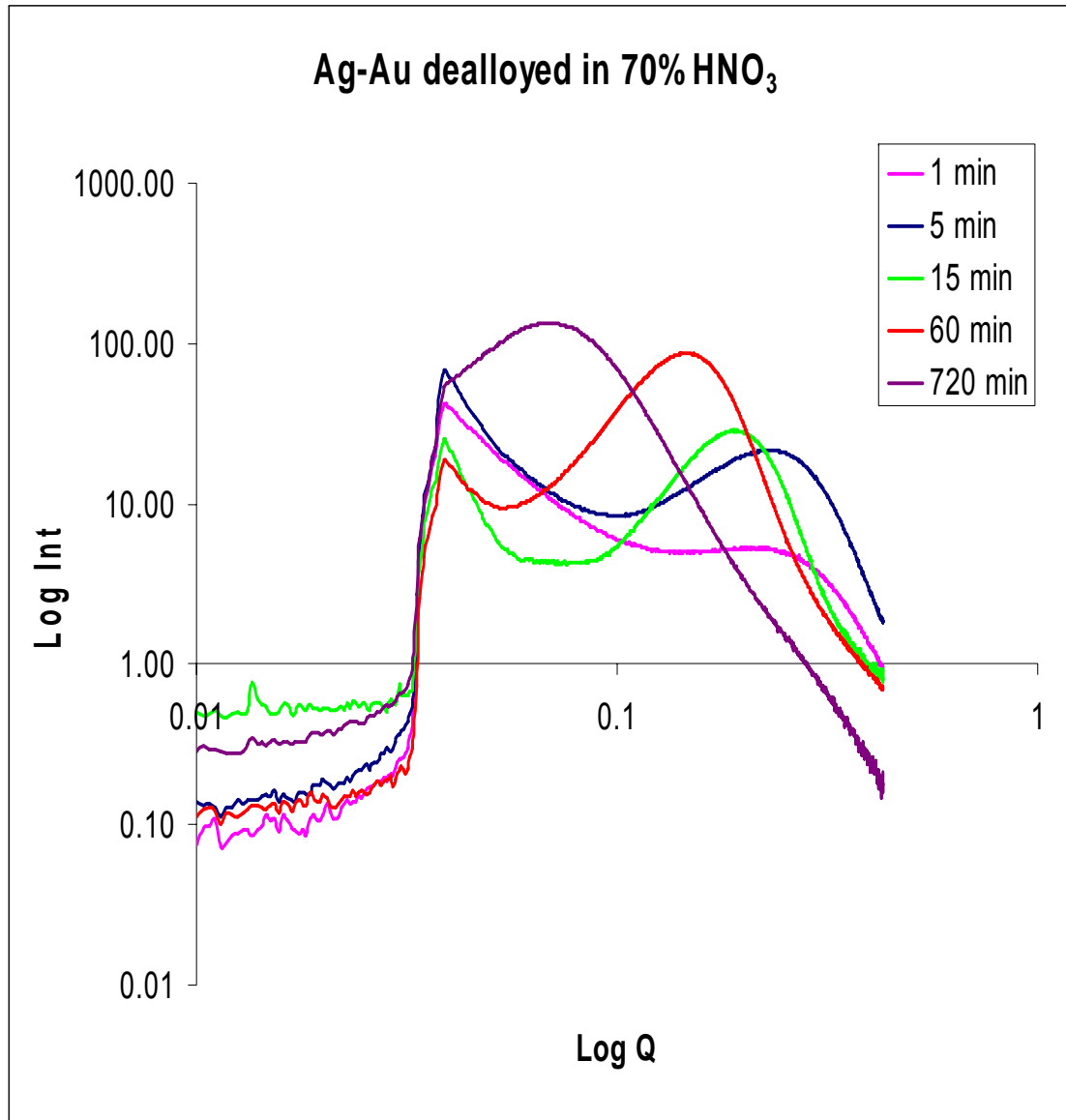


Melted & Sheared



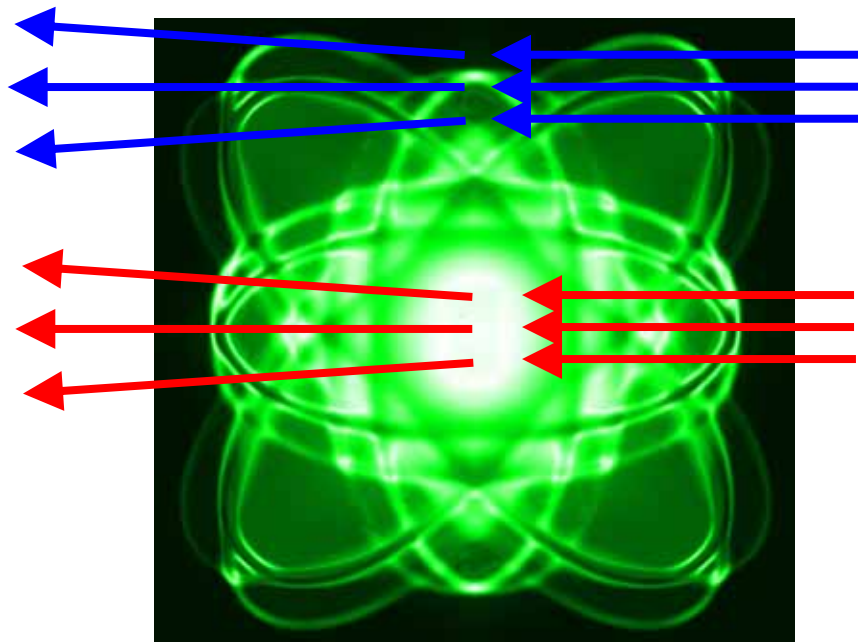
Recrystallized

# Complementary Scattering and Microscopy



Forming a bi-continuous porous network with ligament width on the nanoscale by removing the less noble element from a binary alloy, in this case Ag-Au (multiple films for trans scattering)

## Scattering: Neutrons or Photons?



X-rays

Sensitive to electron density contrast

Neutrons

Sensitive to nuclear scattering length contrast

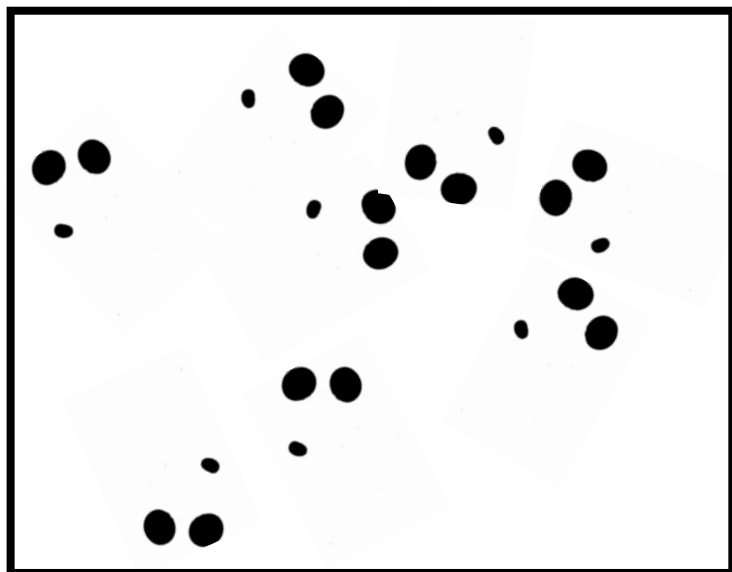
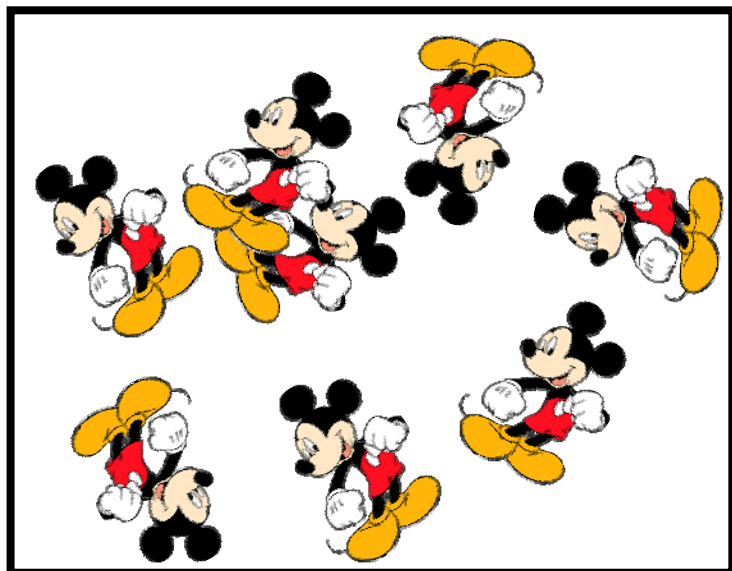
Neutron scattering: Deuteration allows species selection

X-ray scattering:

Relatively small sample quantities required

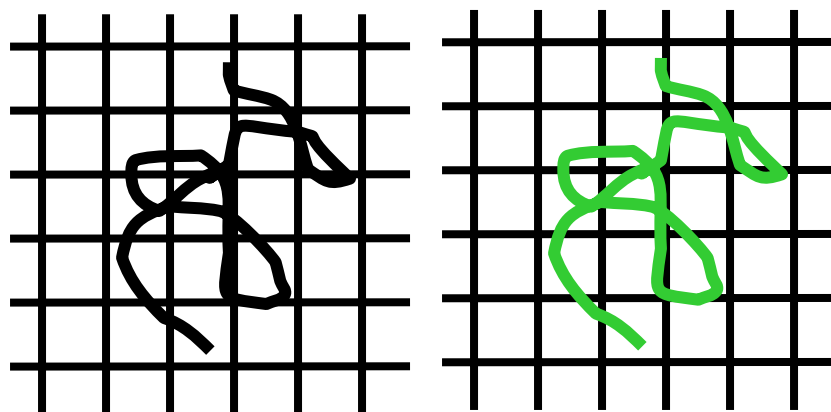
Relatively fast data acquisition times - allows time resolved effects to be characterized

# Scattering: Neutrons or Photons?



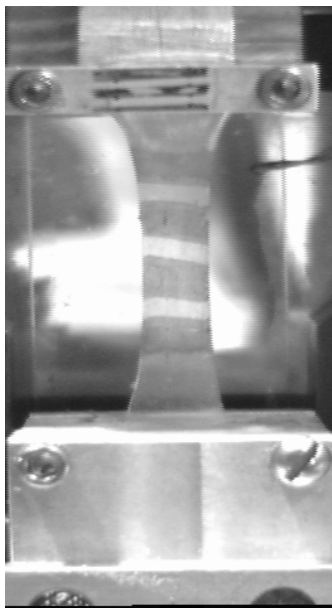
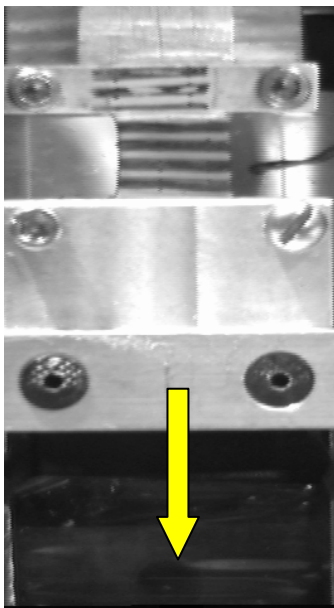
Neutrons: Deuteration  
allows species selection

This essentially permits a dramatic  
alteration to the 'visibility' of the tagged  
elements in terms of their contribution to  
the reciprocal space scattering pattern

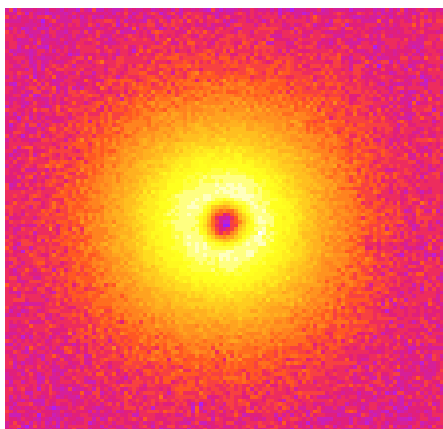


Atom	Scattering length ( $\times 10^{12} \text{ cm}^2$ )	Incoherent scattering ( $\times 10^{24} \text{ cm}^2$ )
■ $^1\text{H}$	-0.374	80
■ $^2\text{D}$	0.667	2

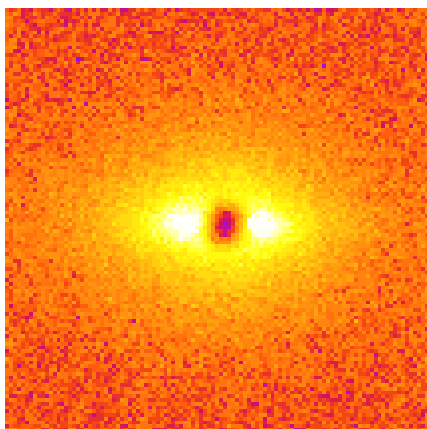
## Scattering: Neutrons or Photons?



Photos of deformation



$\lambda = 0\%$

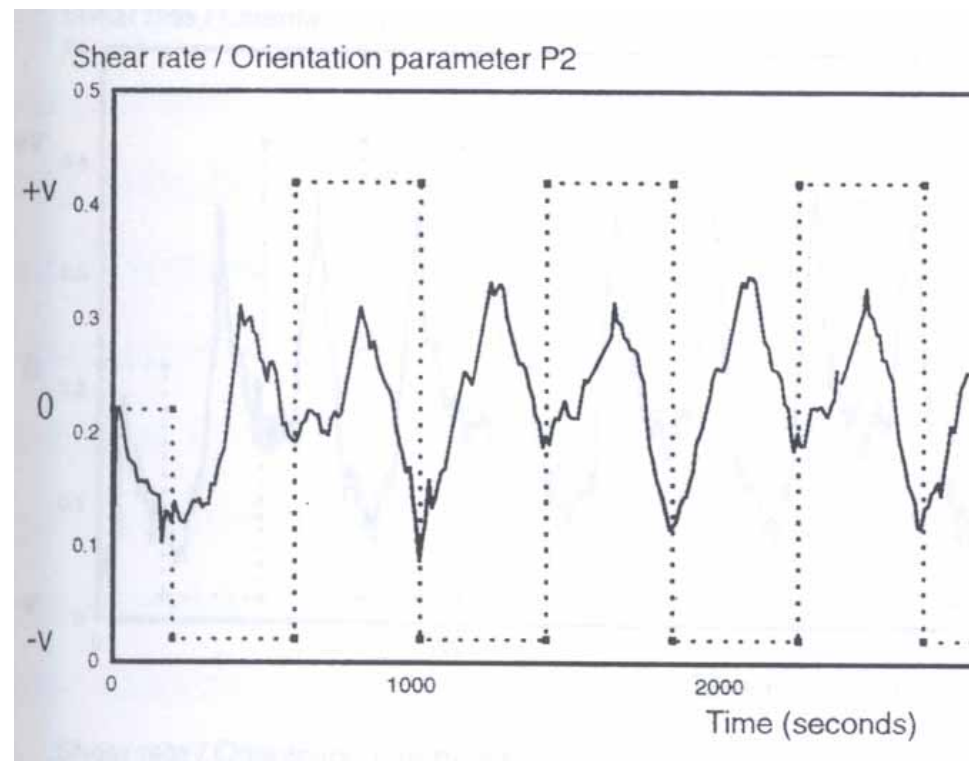
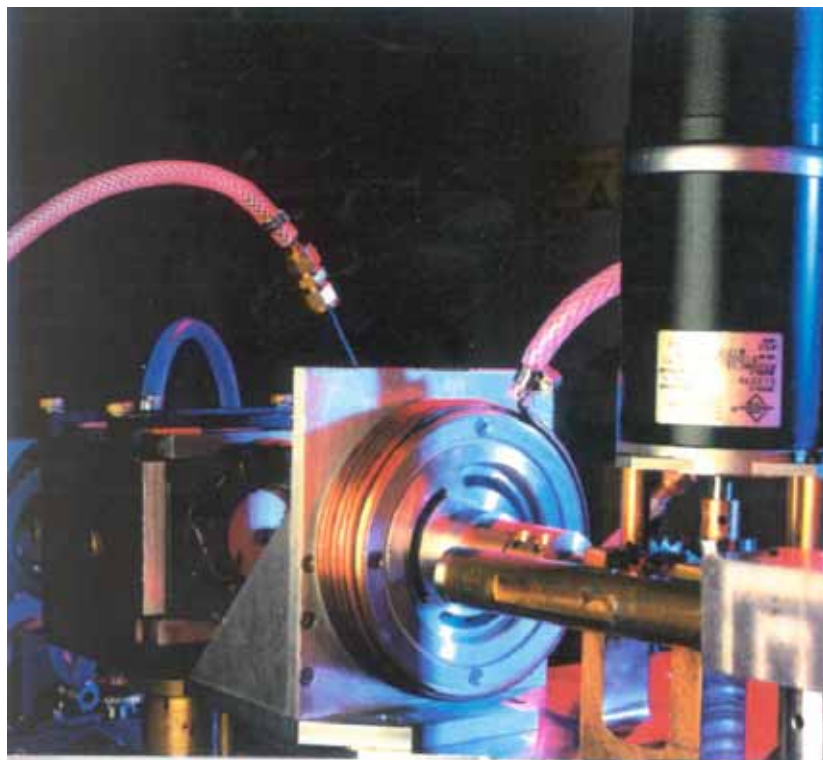


$\lambda = 300\%$

SANS patterns

## Scattering: Neutrons or Photons?

X-rays:           Order of magnitude better spatial resolution  
Fast data acquisition times for time resolved data



Oscillatory Shearing of lyotropic HPC – a liquid crystal polymer

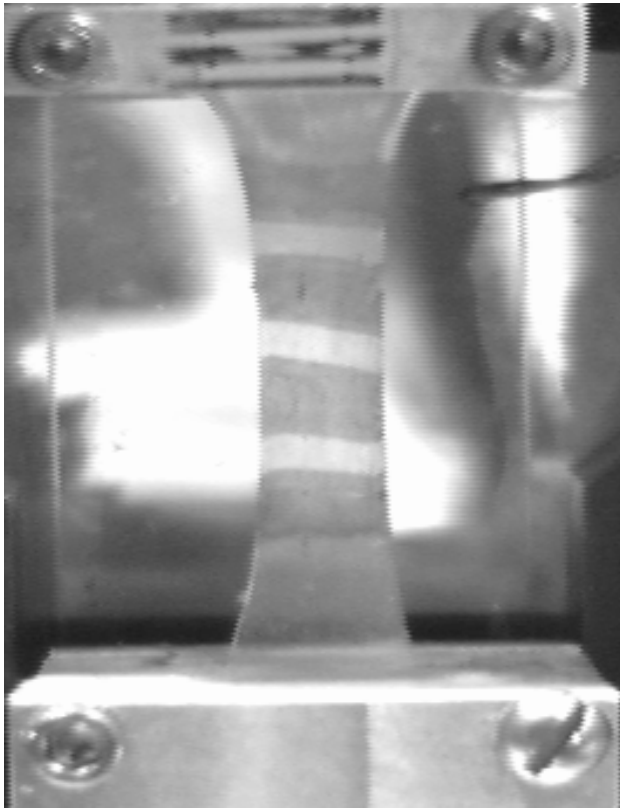
# *X-ray Scattering: Transmission or Reflection?*

Need to be conscious of:

Constituent elements, i.e. absorption cutoffs

Multiple scattering

Area of interest: surface effect or bulk effect



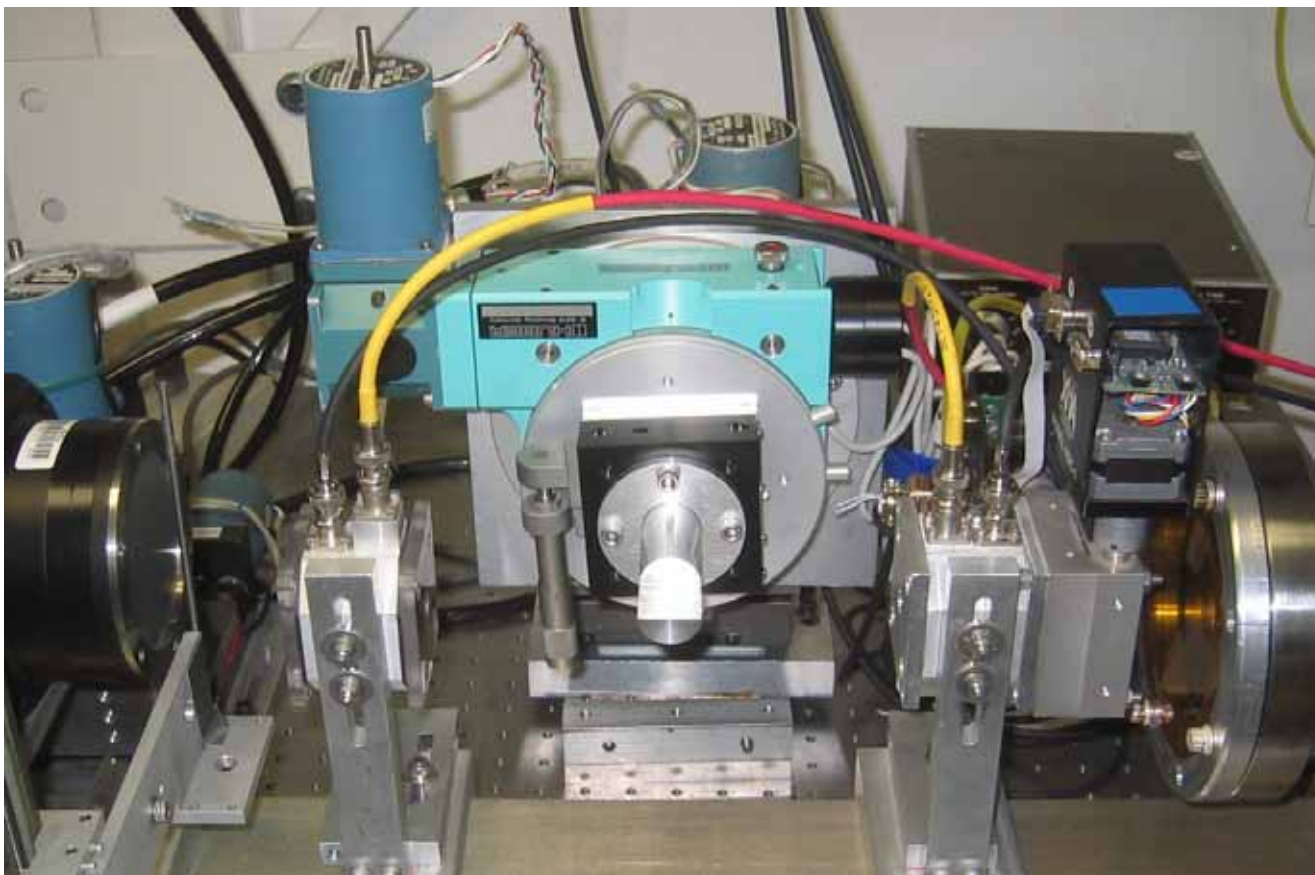
Transmission geometry appropriate for:

- Extracting bulk parameters, especially in deformation
- Weakly scattering samples: can vary path length

## *X-ray Scattering: Transmission or Reflection?*

Reflection geometry appropriate for:

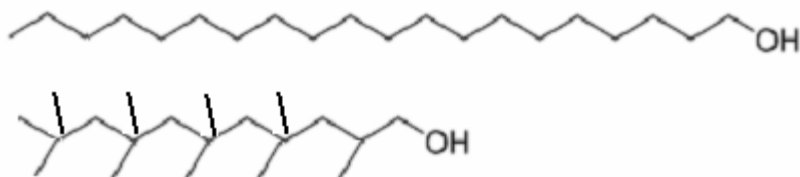
- Films on a substrate (whether opaque or not)
- Probing surface interactions



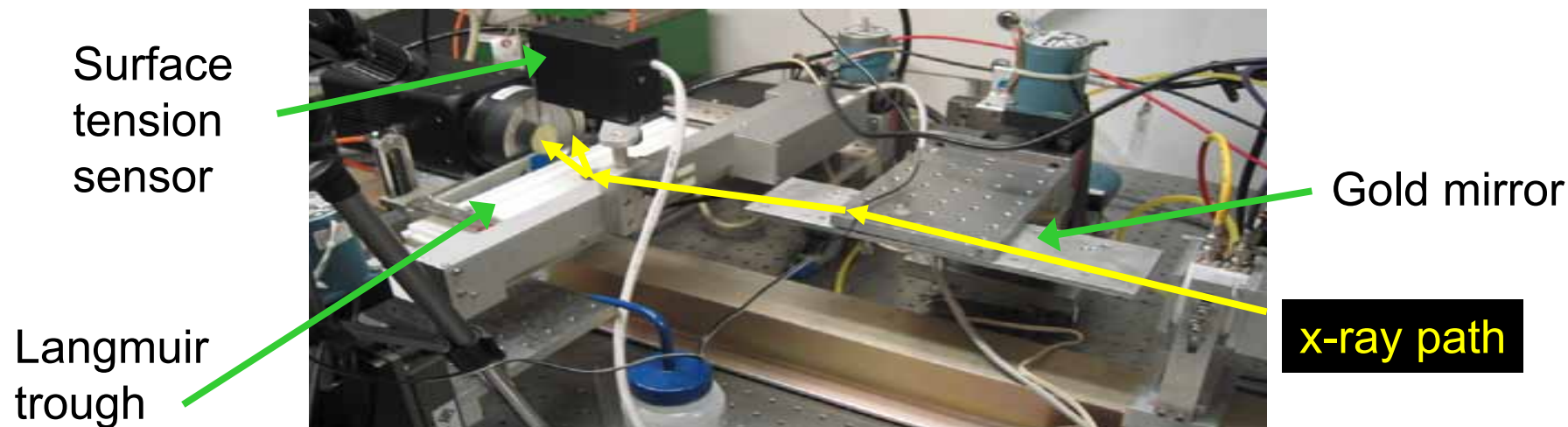
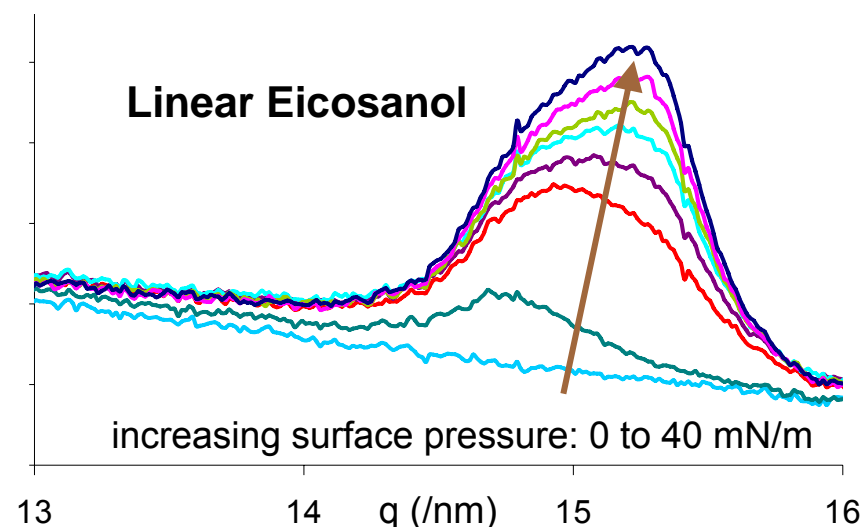
# Rheology of Straight and Branched Fatty Alcohols

Study phase transitions of Langmuir monolayers of mixed fatty alcohols in terms of molecular branching and surface tension

linear eicosanol ( $C_{20}H_{42}O$ , MW = 298)

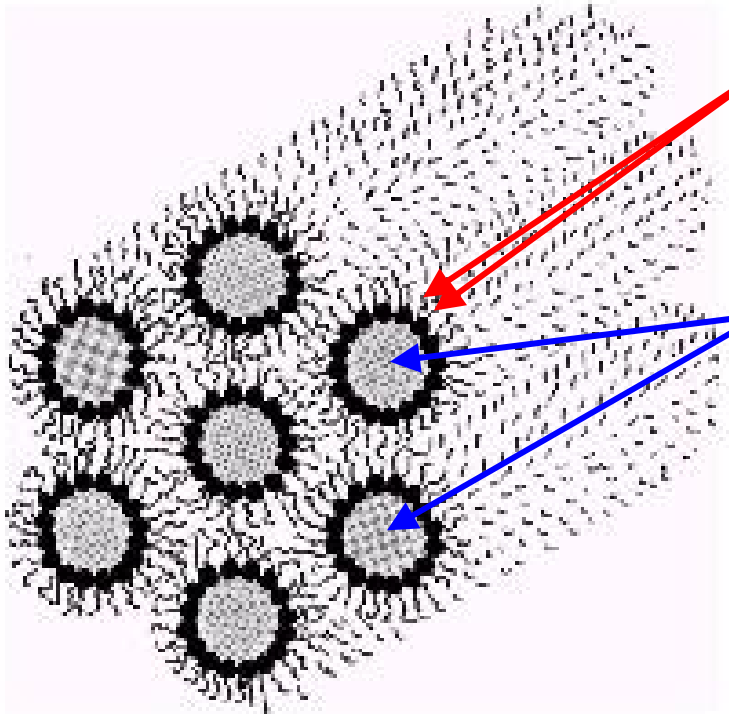


branched eicosanol ( $C_{20}H_{42}O$ , MW = 298)



# *X-ray Scattering: SAXS or WAXS?*

No fundamental difference in physics: a consequence of chemistry



WAXS patterns contain data concerning correlations on an intra-molecular, inter-atomic level

SAXS patterns contain data concerning correlations on an inter-molecular level: necessarily samples where there is macromolecular or aggregate order

As synthesis design/control improves, SAXS becomes more relevant than ever before

# *X-ray Scattering: SAXS or WAXS?*

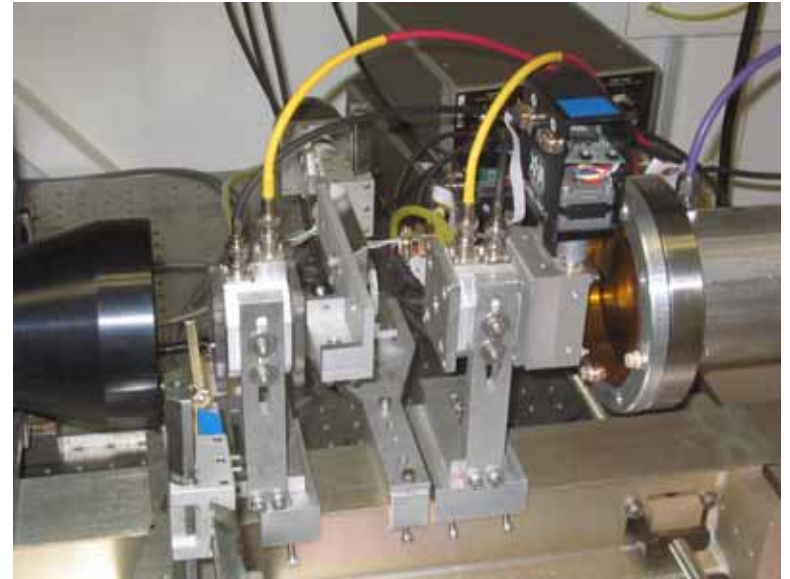
Experimental consequences

WAXS: Detector close to sample, consider:

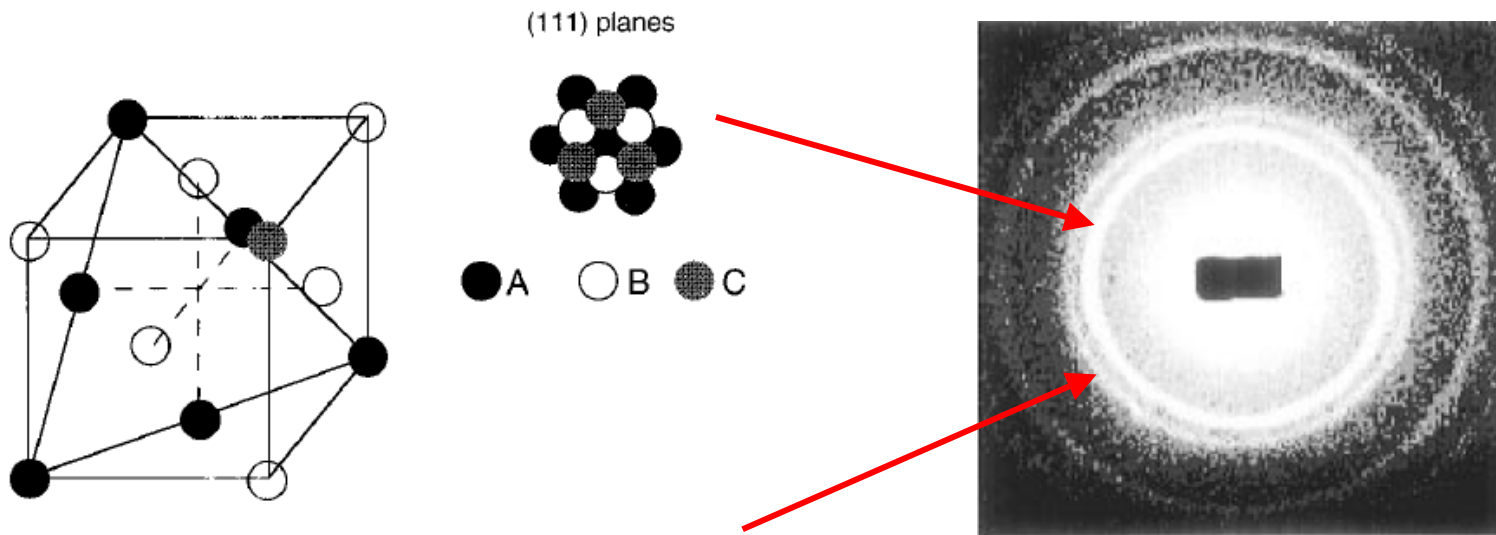
- Distortion of reciprocal space mapping
- Thermal effects when heating sample
- No ion chamber for absorption

SAXS: Detector far from sample, consider:

- Absorption from intermediate space
- Interception of appropriate  $q$  range



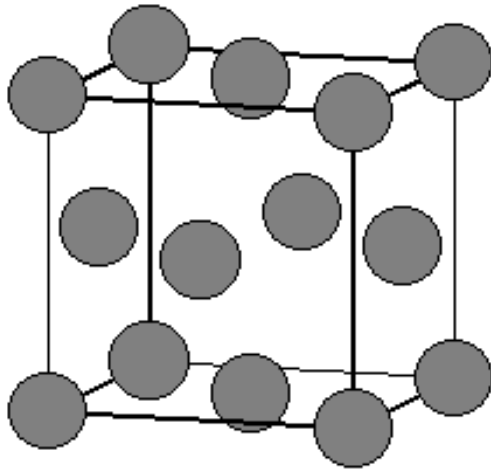
# Recognizing Reciprocal Space Patterns: Indexing



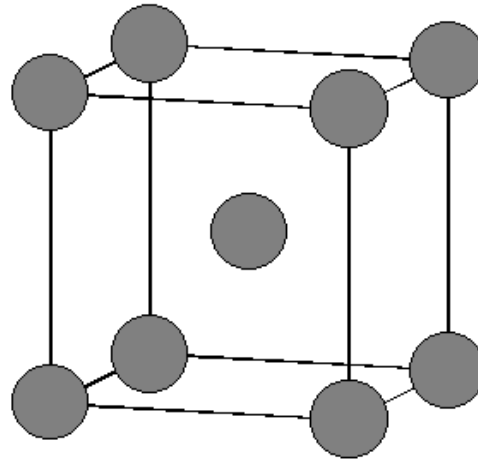
Face centered cubic pattern from diblock copolymer gel

# Recognizing Reciprocal Space Patterns: Indexing

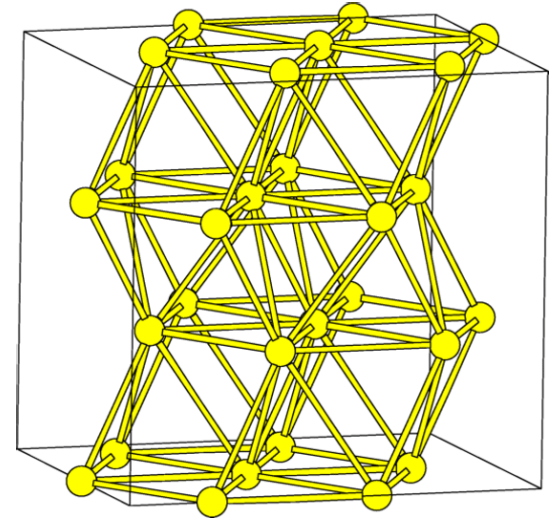
Real  
space  
packing



Face centered cubic



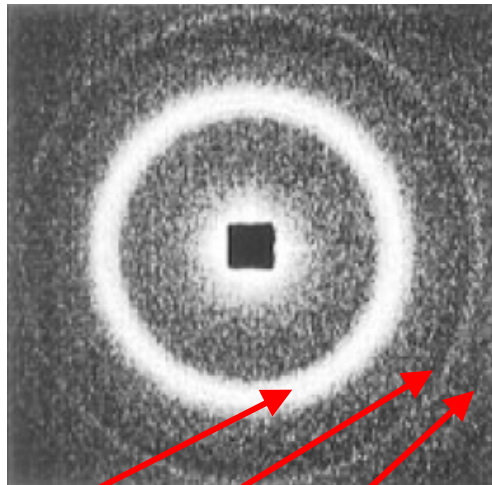
Body centered cubic



Hexagonal

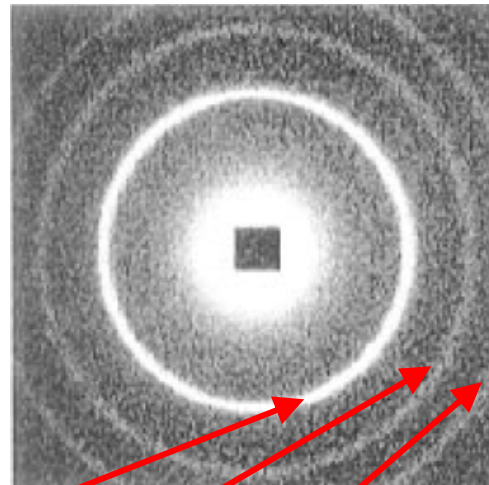
Reciprocal  
space  
image

(unoriented  
domains)

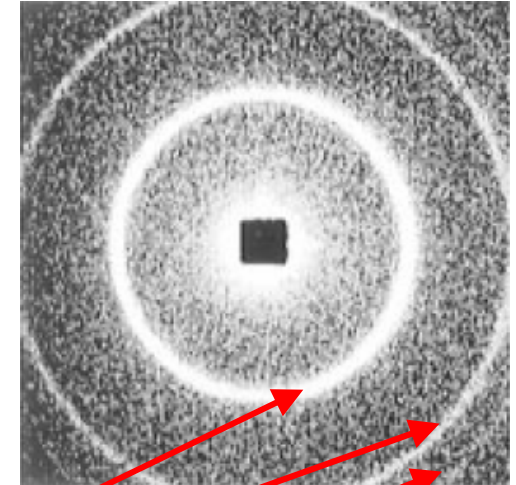


Normalized  
peak positions

$$\equiv 1; \equiv \sqrt{4/3}; \equiv \sqrt{8/3}$$



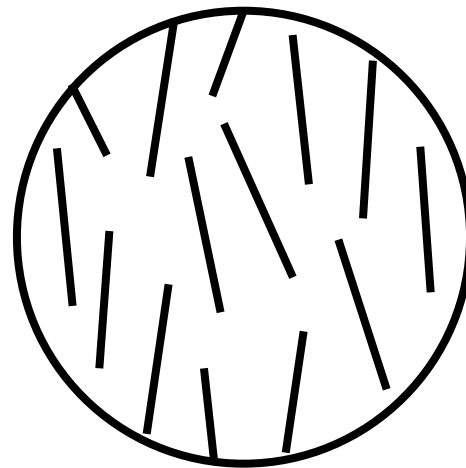
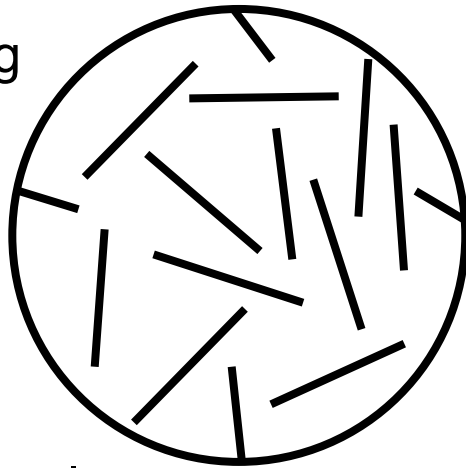
$$\equiv 1; \equiv \sqrt{2}; \equiv \sqrt{3}$$



$$\equiv 1; \equiv \sqrt{3}; \equiv \sqrt{4}$$

# Recognizing Reciprocal Space Patterns: Preferential Orientation

Real  
space  
packing



Reciprocal  
space  
image

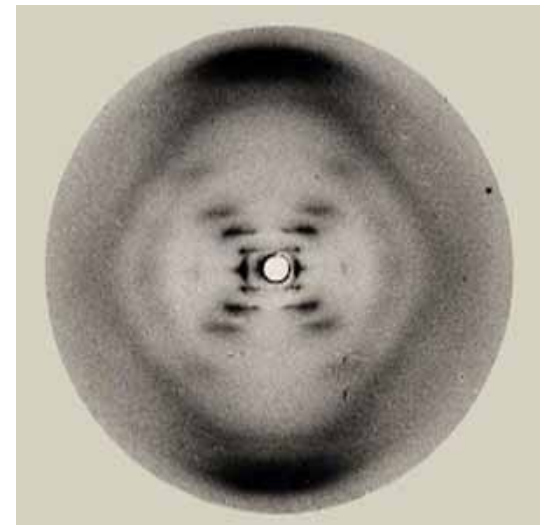
Randomly  
aligned rods



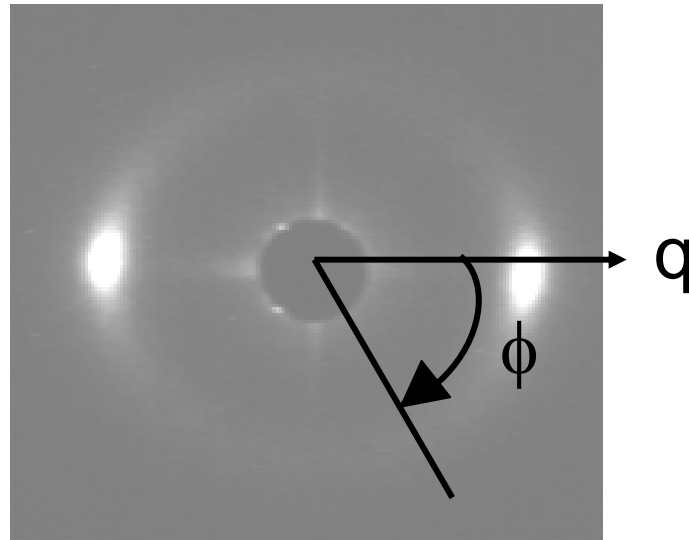
Preferentially  
aligned rods



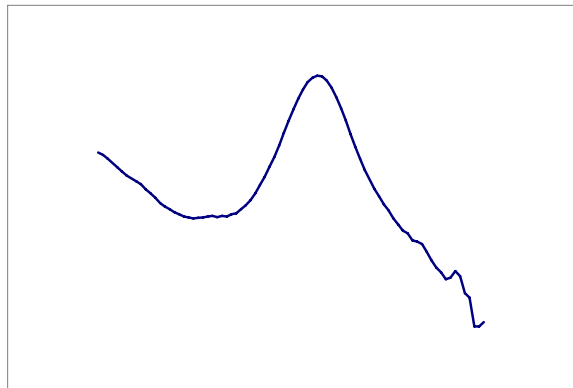
Hydrated DNA



## *Extracting Physical Parameters from X-ray data*

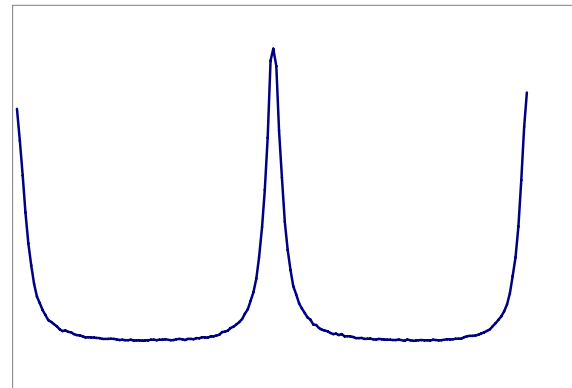


$I(q)$



$q$

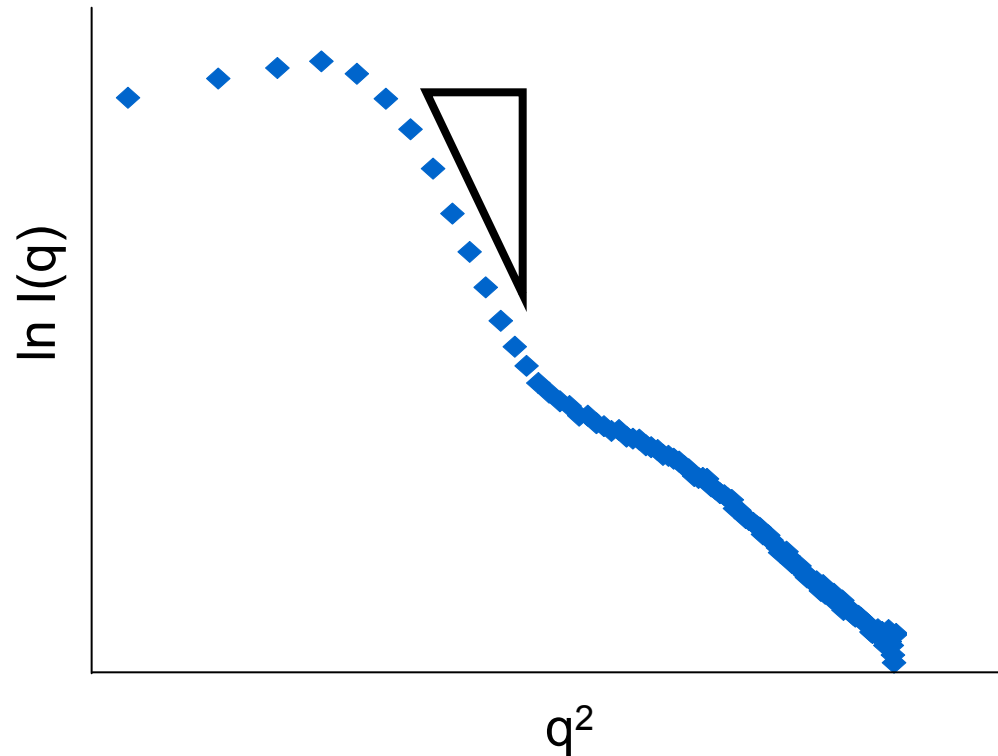
$I(\phi)$



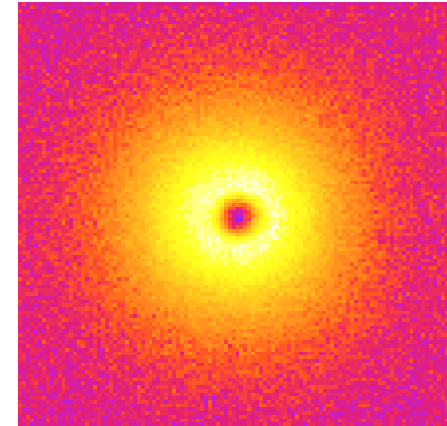
$\phi$

# *Extracting Physical Parameters from X-ray data*

Molecular size: Radius of gyration ( $R_g$ )



**Guinier plot**



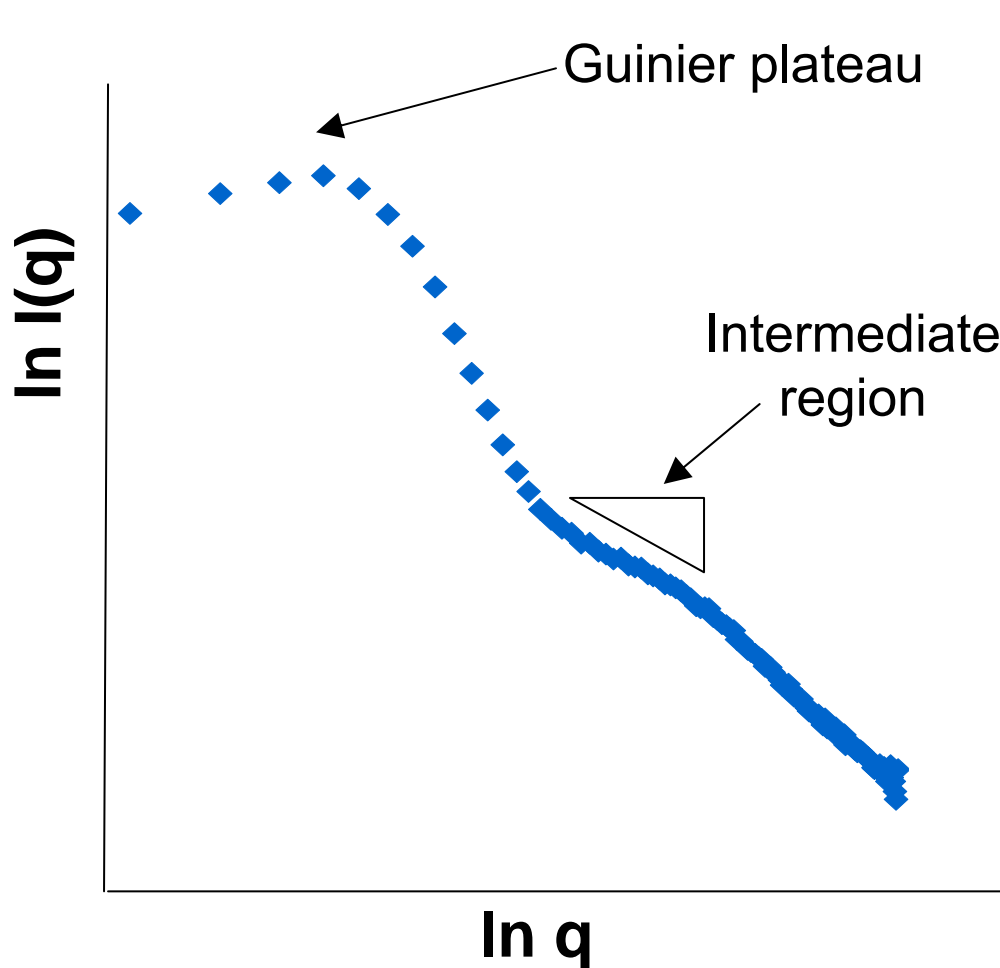
$$I(q) = I(0) \exp [-q^2 R_g^2 / 3]$$

$$R_g^2 \propto \ln I(q) / q^2$$

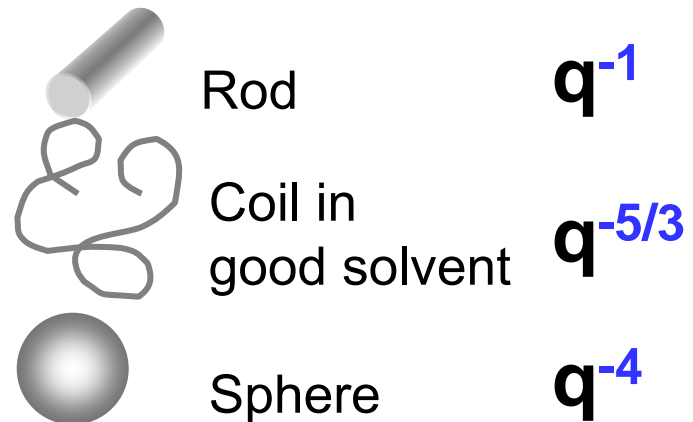
Guinier region:  $q < 1 / R_g$

# Extracting Physical Parameters from X-ray data

## Molecular conformation: Scaling exponent



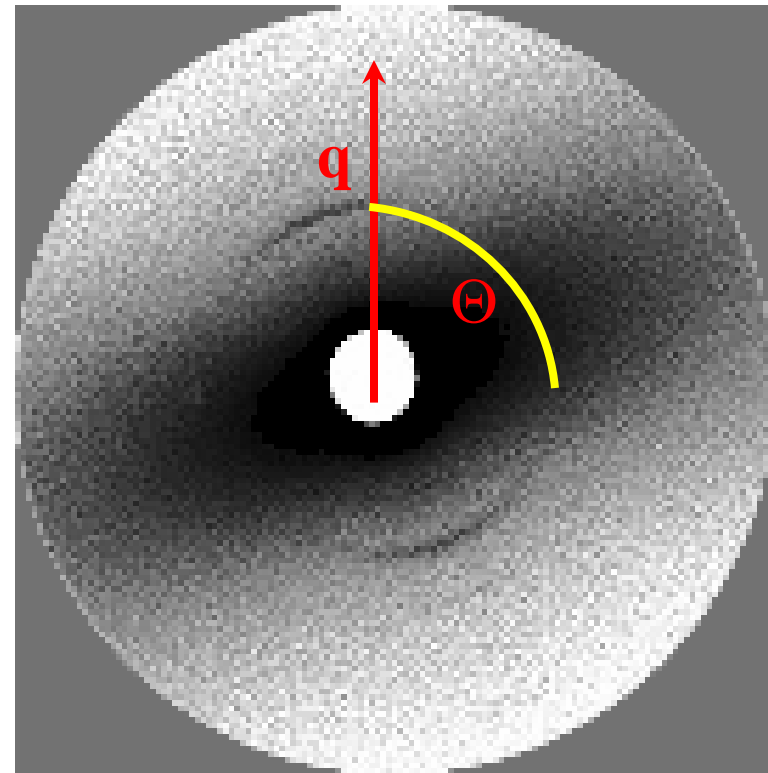
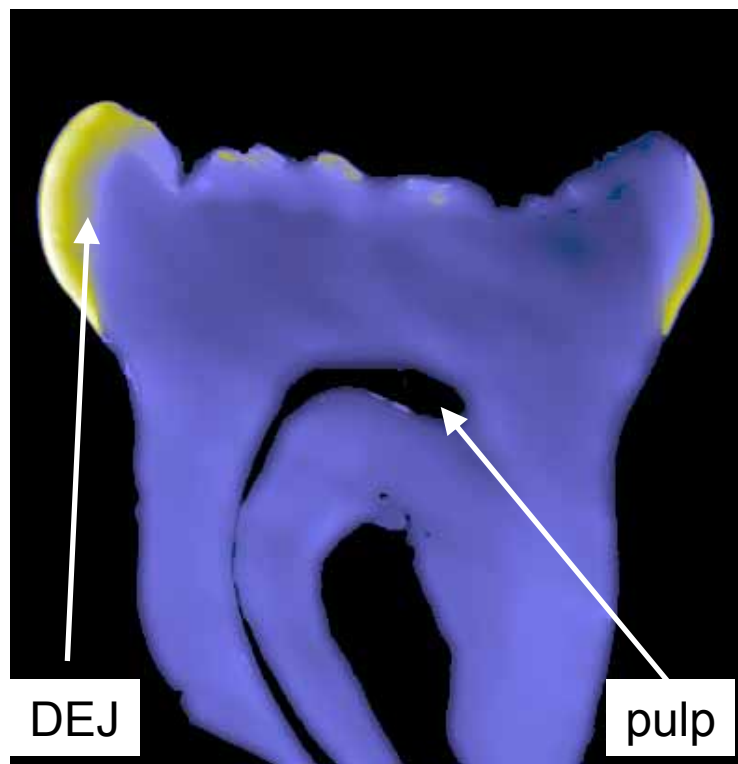
Gradient of profile in intermediate region implies fractal dimension of scattering unit



# Molecular Conformation in Dentin

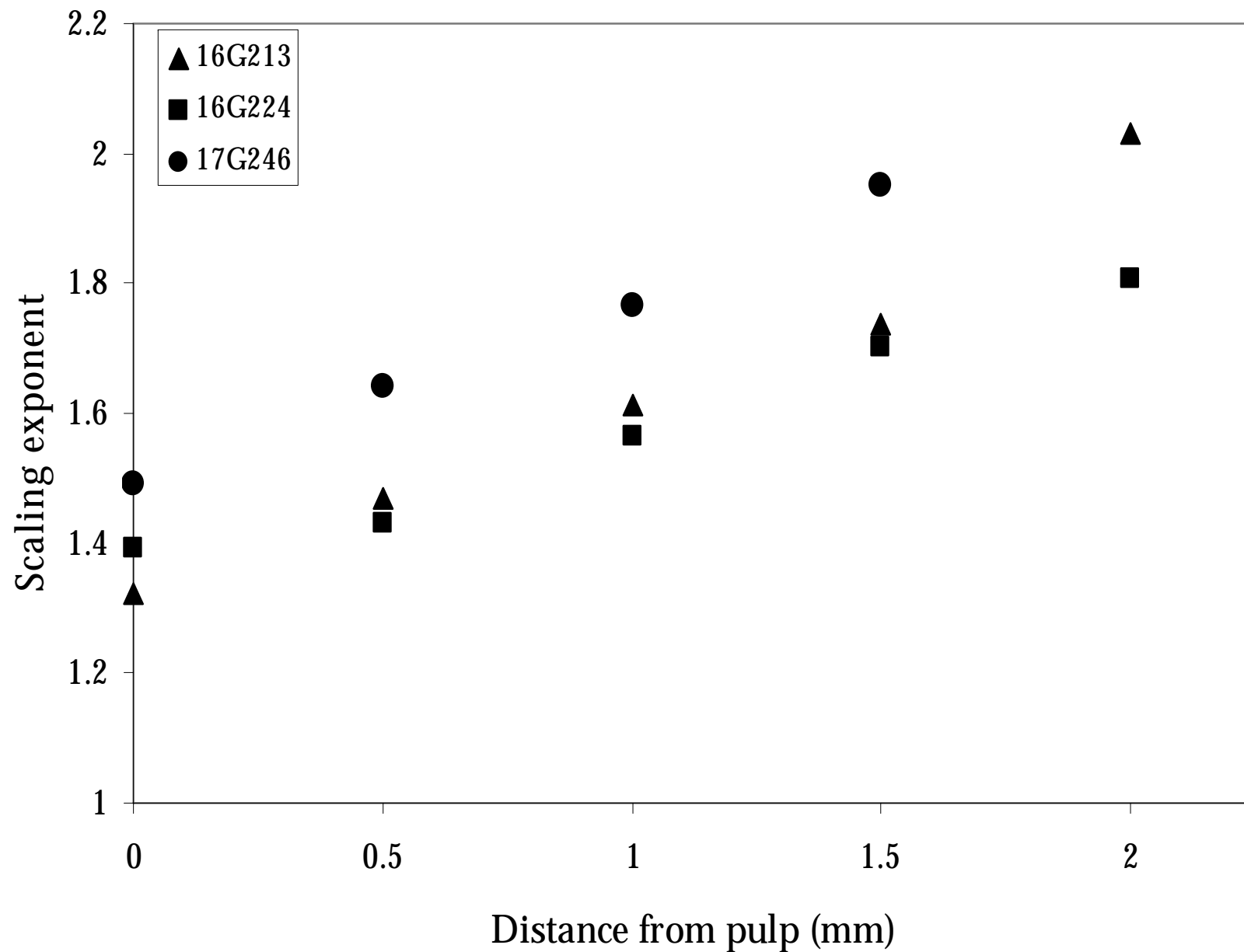
**John H Kinney**

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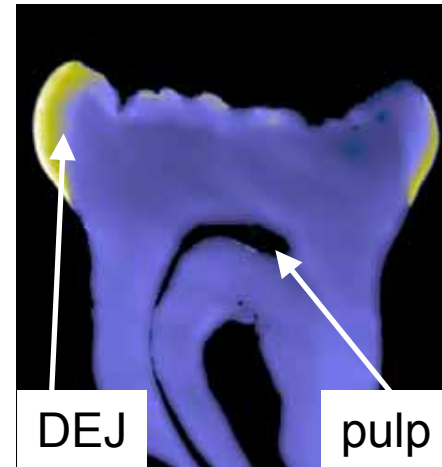
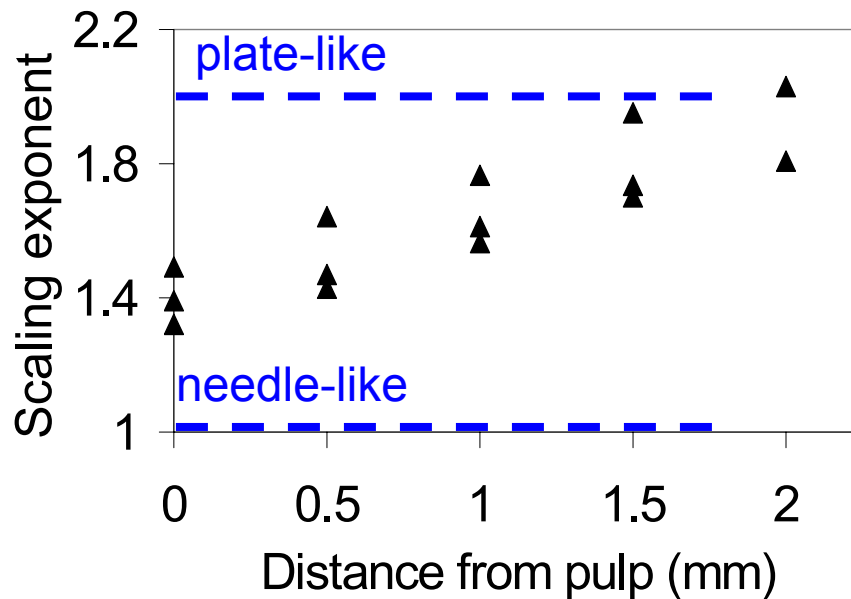
SAXS pattern

## *Molecular Conformation in Dentin*

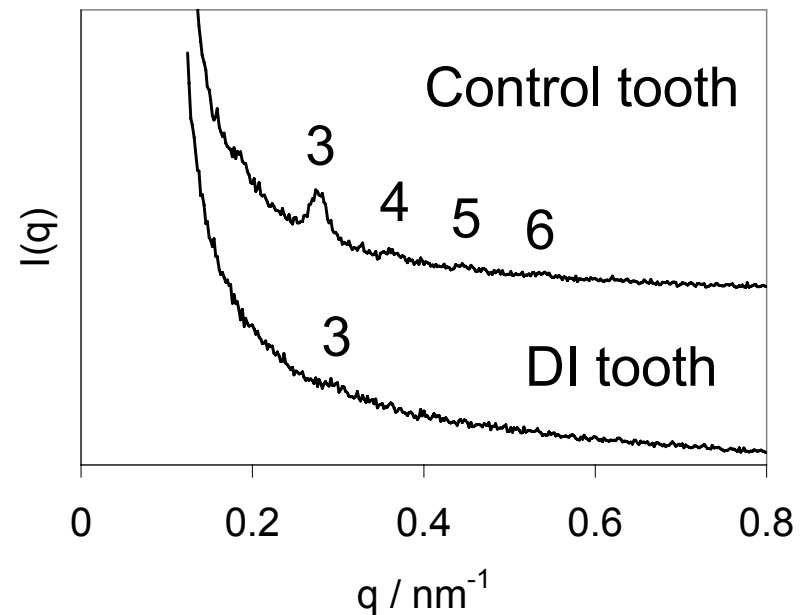


# Molecular Conformation in Dentin

Shape change of mineral crystallites from needle-like to plate-like from pulp to dentin-enamel junction (DEJ).

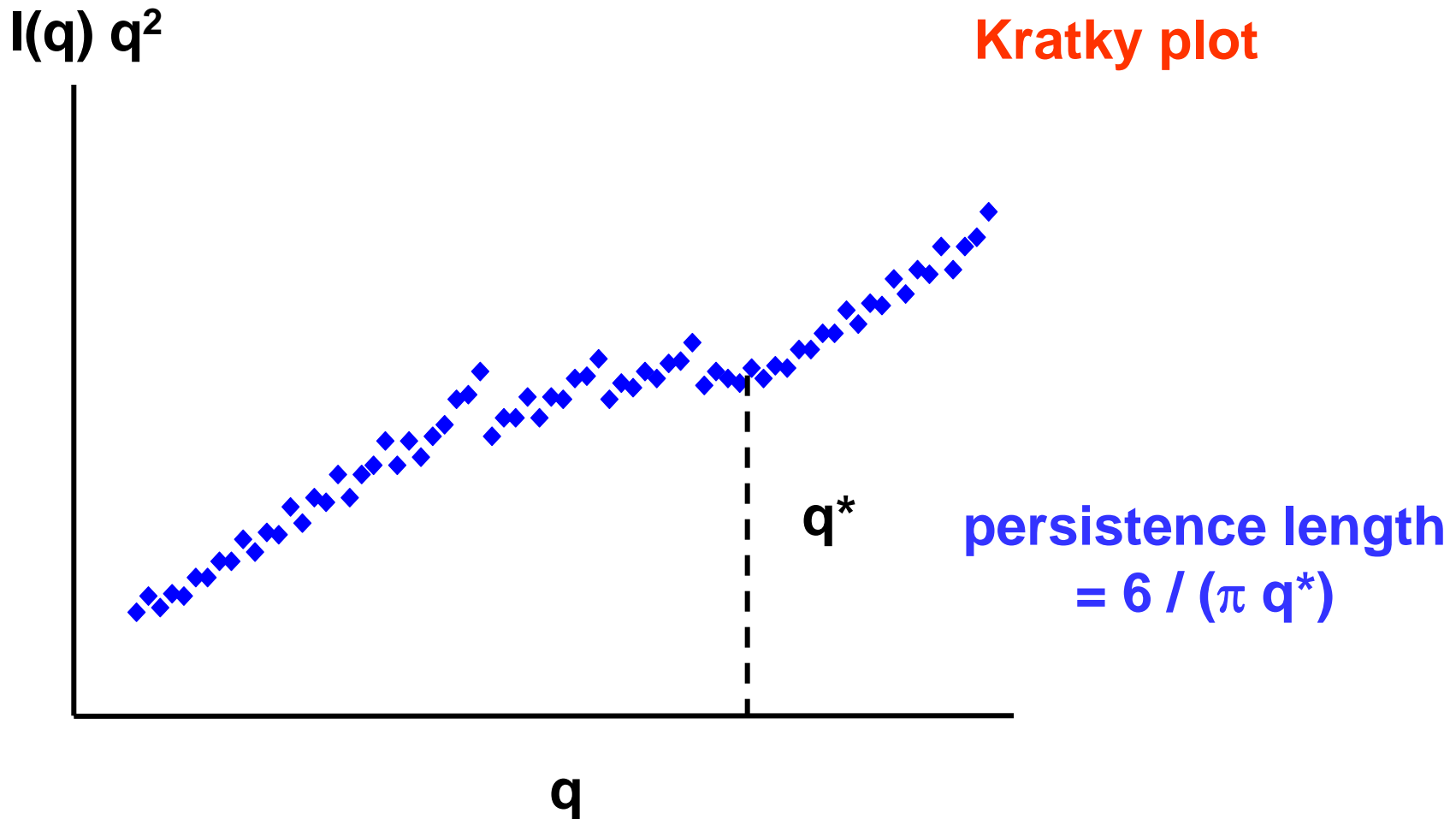


Dentinogenesis imperfecta (DI) teeth shown to exhibit impaired development of intrafibrillar mineral: characteristic scattering peaks are absent from the diseased tooth.



# *Extracting Physical Parameters from X-ray data*

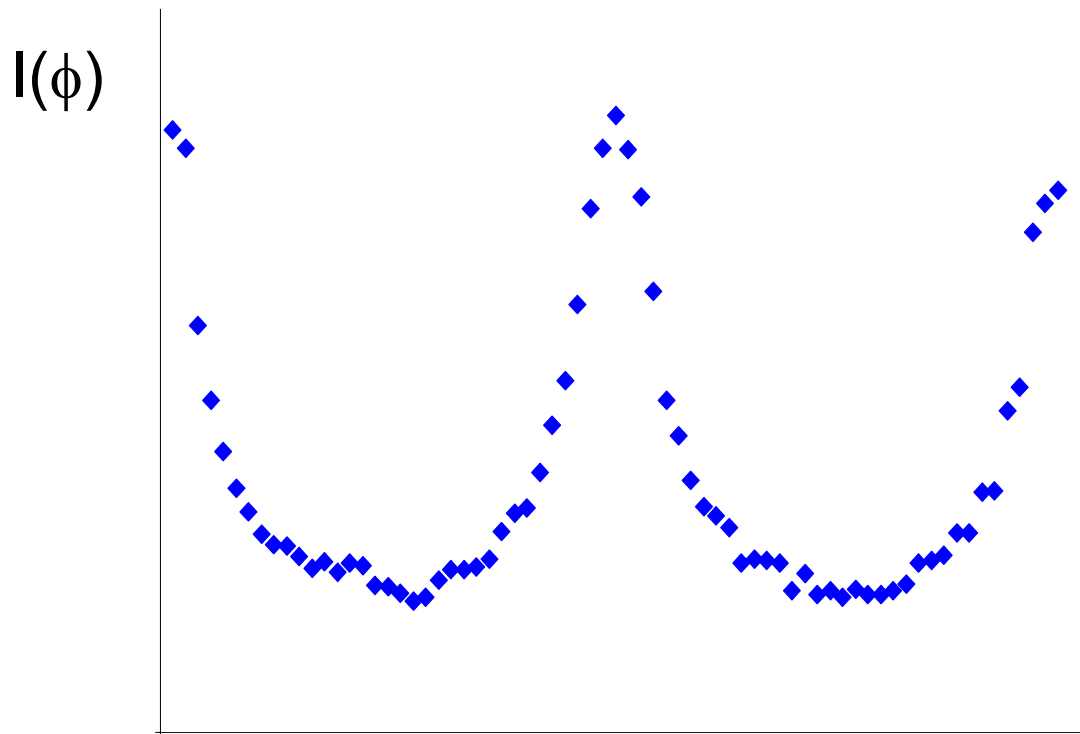
Molecular conformation: Persistence length of coiled chain



# Extracting Physical Parameters from X-ray data

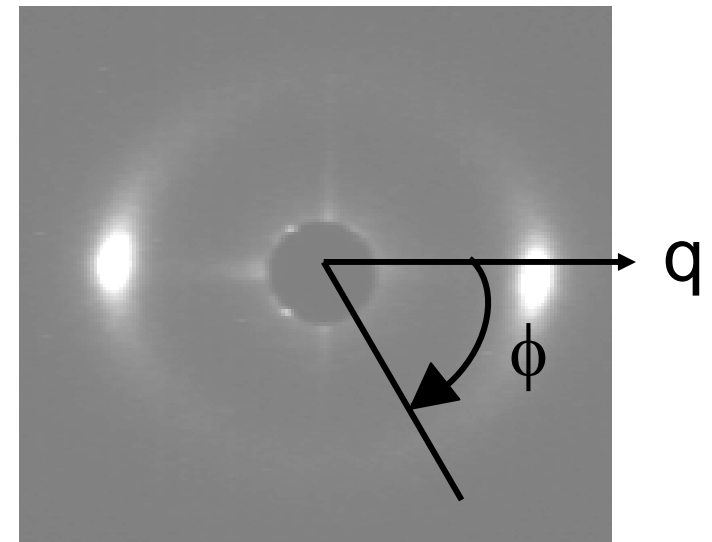
Molecular orientation: Orientation parameter  $P_2$

$$\langle P_{2n}(\cos \phi) \rangle = \frac{\int I(s, \phi) P_{2n}(\cos \phi) \sin \phi d\phi}{\int I(s, \phi) \sin \phi d\phi}$$



**Azimuthal profile**  $\phi$

Normalized:  
 $-0.5 < P_2 < 1$



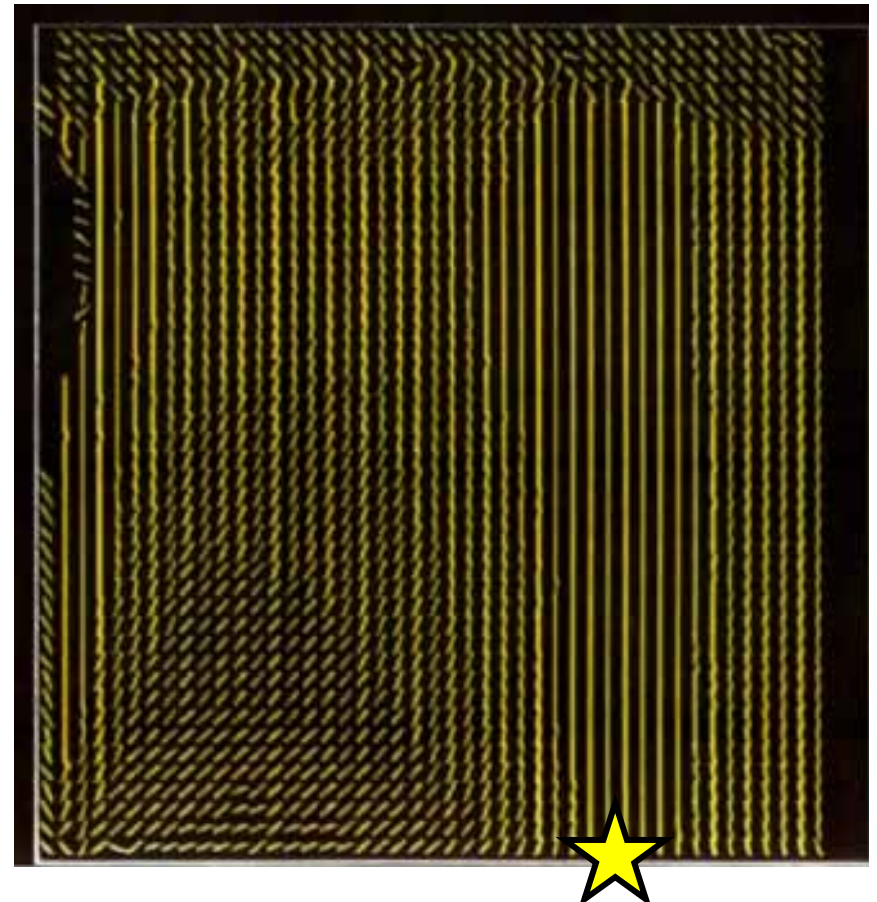
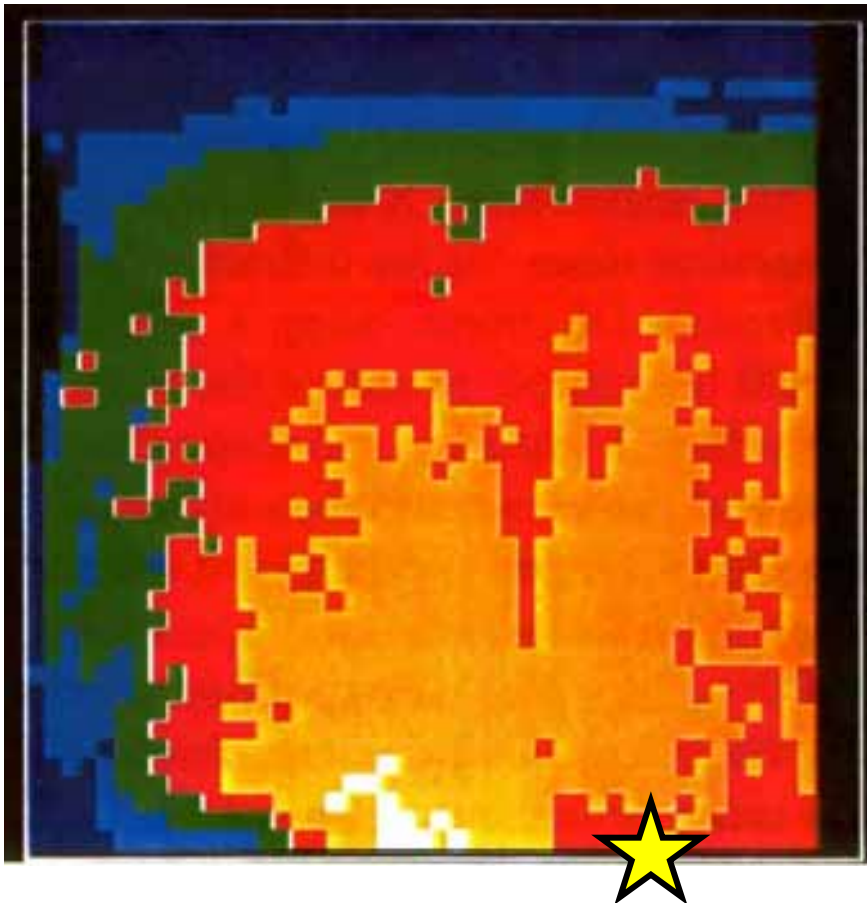
# *Molecular Orientation in Injection Moldings*

Measuring the degree and inclination of preferential molecular orientation in a piece of injection molded plastic (e.g. hip replacement joints). ~ 1500 WAXS patterns

★ Marks the injection point

Orientation parameters:  $0 < P_2 < 0.3$

Axis of orientation



## *SSRL Beamline 1-4: SAXS Materials Science*

