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> restart
>  $\Delta H_{mix} := -25000$ ;  $\Delta Hel := -109300$ ;  $\gamma A := 0.636$ ;  $\gamma B := 0.805$ ;  $\sigma := 31217$ ;  $z := 8$ ;  $R := 8.31$ ;  $\alpha := \frac{5}{6}$ ;  $v := \frac{1}{2}$ ;  $t := 0.4$ ;  $X0 := 0.04$ ;  $T := 900 + 273$ 
 $\Delta H_{mix} := -25000$ 
 $\Delta Hel := -109300$ 
 $\gamma A := 0.636$ 
 $\gamma B := 0.805$ 
 $\sigma := 31217$ 
 $z := 8$ 
 $R := 8.31$ 
 $\alpha := \frac{5}{6}$ 
 $v := \frac{1}{2}$ 
 $t := 0.4$ 
 $X0 := 0.04$ 
 $T := 1173$  (1)

>  $\omega := \frac{4 \cdot \Delta H_{mix}}{z}$ 
 $\omega := -12500$  (2)

>  $eq1 := \omega \cdot z \cdot (1 - 2 \cdot Xb) \cdot (1 - fig) + \alpha \cdot \omega \cdot v \cdot z \cdot (1 - 2 \cdot Xig) \cdot fig + v \cdot \sigma \cdot (\gamma A - \gamma B) \cdot fig + R \cdot T \cdot (\ln(Xb) - \ln(1 - Xb)) \cdot (1 - fig) - \lambda \cdot (1 - fig)$ 
 $eq1 := -100000 (1 - 2 Xb) (1 - fig) - \frac{125000}{3} (1 - 2 Xig) fig - 2637.836500 fig + 9747.63 (\ln(Xb) - \ln(1 - Xb)) (1 - fig) - \lambda (1 - fig)$  (3)

>  $eq2 := \alpha \cdot \omega \cdot v \cdot z \cdot (1 - 2 \cdot Xb) \cdot fig + v \cdot \sigma \cdot (\gamma A - \gamma B) \cdot fig + \alpha \cdot \omega \cdot (1 - 2 \cdot v) \cdot z \cdot (1 - 2 \cdot Xig) \cdot fig + (1 - 2 \cdot v) \cdot \sigma \cdot (\gamma A - \gamma B) \cdot fig + \Delta Hel \cdot fig + R \cdot T \cdot (\ln(Xig) - \ln(1 - Xig)) \cdot fig - \lambda \cdot fig$ 
 $eq2 := -\frac{125000}{3} (1 - 2 Xb) fig - 1.119378365 10^5 fig + 9747.63 (\ln(Xig) - \ln(1 - Xig)) fig - \lambda fig$  (4)

>  $eq3 := -\omega \cdot z \cdot Xb \cdot (1 - Xb) + \alpha \cdot \omega \cdot v \cdot z \cdot (Xb \cdot (1 - Xig) + Xig \cdot (1 - Xb)) + v \cdot \sigma \cdot ((Xb + Xig) \cdot \gamma A + (1 - Xb + 1 - Xig) \cdot \gamma B) + \alpha \cdot \omega \cdot (1 - 2 \cdot v) \cdot z \cdot Xig \cdot (1 - Xig) + (1 - 2 v) \cdot \sigma \cdot (Xig \cdot \gamma A + (1 - Xig) \cdot \gamma B) + Xig \cdot \Delta Hel - R \cdot T \cdot (Xb \cdot \ln(Xb) + (1 - Xb) \cdot \ln(1 - Xb)) + R \cdot T \cdot (Xig \cdot \ln(Xig) + (1 - Xig) \cdot \ln(1 - Xig)) - \lambda \cdot (Xig - Xb)$ 
 $eq3 := 100000 Xb (1 - Xb) - \frac{125000}{3} Xb (1 - Xig) - \frac{125000}{3} Xig (1 - Xb) - 2637.836500 Xb - 1.119378365 10^5 Xig + 25129.68500 - 9747.63 Xb \ln(Xb) - 9747.63 (1 - Xb) \ln(1 - Xb) + 9747.63 Xig \ln(Xig) + 9747.63 (1 - Xig) \ln(1 - Xig) - \lambda (Xig - Xb)$  (5)

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$$\begin{aligned} > \text{eq4} := Xb \cdot (1 - \text{fig}) + Xig \cdot \text{fig} - X0 \\ &\quad \text{eq4} := Xb (1 - \text{fig}) + Xig \cdot \text{fig} - 0.04 \end{aligned} \tag{6}$$

$$\begin{aligned} > \lambda_s := \text{solve}(\text{eq2} = 0, \lambda) \\ \lambda_s := -1.536045032 \cdot 10^5 + 83333.33333 Xb + 9747.630000 \ln(Xig) - 9747.630000 \ln(1. \\ &\quad - 1. Xig) \end{aligned} \tag{7}$$

$$\begin{aligned} > \text{eq1} := \text{subs}(\lambda = \lambda_s, \text{eq1}) \\ \text{eq1} := -100000 (1 - 2 Xb) (1 - \text{fig}) - \frac{125000}{3} (1 - 2 Xig) \text{fig} - 2637.836500 \text{fig} \end{aligned} \tag{8}$$

$$\begin{aligned} &\quad + 9747.63 (\ln(Xb) - \ln(1 - Xb)) (1 - \text{fig}) - (-1.536045032 \cdot 10^5 + 83333.33333 Xb \\ &\quad + 9747.630000 \ln(Xig) - 9747.630000 \ln(1. - 1. Xig)) (1 - \text{fig}) \end{aligned}$$

$$\begin{aligned} > \text{eq3} := \text{subs}(\lambda = \lambda_s, \text{eq3}) \\ \text{eq3} := 100000 Xb (1 - Xb) - \frac{125000}{3} Xb (1 - Xig) - \frac{125000}{3} Xig (1 - Xb) \end{aligned} \tag{9}$$

$$\begin{aligned} &\quad - 2637.836500 Xb - 1.119378365 \cdot 10^5 Xig + 25129.68500 - 9747.63 Xb \ln(Xb) \\ &\quad - 9747.63 (1 - Xb) \ln(1 - Xb) + 9747.63 Xig \ln(Xig) + 9747.63 (1 - Xig) \ln(1 - Xig) \\ &\quad - (-1.536045032 \cdot 10^5 + 83333.33333 Xb + 9747.630000 \ln(Xig) - 9747.630000 \ln(1. \\ &\quad - 1. Xig)) (Xig - Xb) \end{aligned}$$

$$\begin{aligned} > \text{sol} := \text{fsolve}(\{\text{eq1} = 0, \text{eq3} = 0, \text{eq4} = 0\}, \{Xb = 0 .. 1, Xig = 0 .. 1, \text{fig} = 0 .. 1\}) \\ \text{sol} := \{Xb = 0.02946935418, Xig = 0.9165972538, \text{fig} = 0.01187049334\} \end{aligned} \tag{10}$$

$$\begin{aligned} > Xb := \text{subs}(\text{sol}[1], Xb) \\ Xb := 0.02946935418 \end{aligned} \tag{11}$$

$$\begin{aligned} > Xig := \text{subs}(\text{sol}[2], Xig) \\ Xig := 0.9165972538 \end{aligned} \tag{12}$$

$$\begin{aligned} > \text{fig} := \text{subs}(\text{sol}[3], \text{fig}) \\ \text{fig} := 0.01187049334 \end{aligned} \tag{13}$$

$$\begin{aligned} > \text{eq5} := \text{fig} - 1 + \left(\frac{d - t}{d} \right)^3 \\ \text{eq5} := -0.9881295067 + \frac{(d - 0.4)^3}{d^3} \end{aligned} \tag{14}$$

$$\begin{aligned} > d := \text{fsolve}(\text{eq5} = 0, d) \\ d := 100.6899353 \end{aligned} \tag{15}$$

$$\begin{aligned} > \text{Gamma} := \frac{(Xig - Xb)}{\sigma \cdot (1 - Xb)} \\ \Gamma := 0.00002928099429 \end{aligned} \tag{16}$$

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