

*Annual Review of Biophysics***Physical Principles Underlying  
the Complex Biology of  
Intracellular Phase Transitions****Jeong-Mo Choi,<sup>1,2,3</sup> Alex S. Holehouse,<sup>1,2</sup>  
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Annu. Rev. Biophys. 2020. 49:107–33

First published as a Review in Advance on  
January 31, 2020

The *Annual Review of Biophysics* is online at  
[biophys.annualreviews.org](http://biophys.annualreviews.org)

<https://doi.org/10.1146/annurev-biophys-121219-081629>

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**Keywords**

phase separation, phase transition, biomolecular condensates, stickers and spacers

**Abstract**

Many biomolecular condensates appear to form via spontaneous or driven processes that have the hallmarks of intracellular phase transitions. This suggests that a common underlying physical framework might govern the formation of functionally and compositionally unrelated biomolecular condensates. In this review, we summarize recent work that leverages a stickers-and-spacers framework adapted from the field of associative polymers for understanding how multivalent protein and RNA molecules drive phase transitions that give rise to biomolecular condensates. We discuss how the valence of stickers impacts the driving forces for condensate formation and elaborate on how stickers can be distinguished from spacers in different contexts. We touch on the impact of sticker- and spacer-mediated interactions on the rheological properties of condensates and show how the model can be mapped to known drivers of different types of biomolecular condensates.

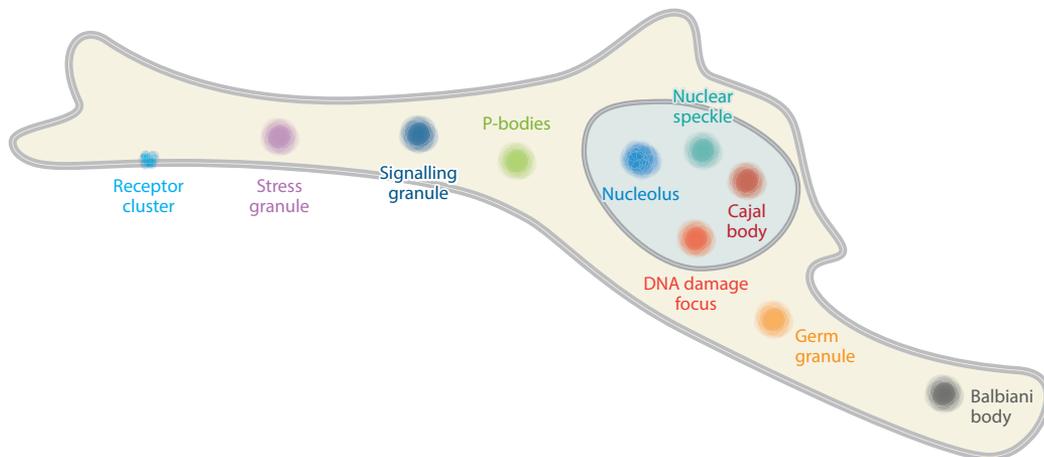
## Contents

INTRODUCTION .....	108
Concepts of Solvent Quality and Findings from Mean-Field Theories .....	109
Going Beyond Homopolymers .....	110
MEAN-FIELD INCARNATION OF THE STICKERS-AND-SPACERS	
MODEL .....	111
An Obligate Heterotypic-Interaction Model for Stickers and Spacers .....	113
Extending the Obligate Heterotypic Model to Include Homotypic	
Sticker Interactions .....	114
What if We Have Multiple Types of Stickers in Our System? .....	115
Effects of Spacers .....	115
IDENTIFYING STICKERS VERSUS SPACERS .....	117
Spectroscopic Routes to Identifying Stickers Versus Spacers .....	117
Apparent Valence Versus Effective Valence of Stickers .....	118
CONTRIBUTIONS OF STICKER-STICKER CROSSLINKS AND SPACER	
EXCLUDED VOLUMES TO STRUCTURAL AND DYNAMICAL	
PROPERTIES OF CONDENSATES .....	119
Is the Distinction Between Viscous and Viscoelastic Network Fluids Relevant	
or of Functional Importance? .....	120
Connecting Dynamic Moduli to Internal Structures Within Condensates .....	121
THE STICKERS-AND-SPACERS MODEL IN BIOLOGICAL SYSTEMS .....	121
EMERGENT VERSUS INTRINSIC STICKERS .....	123
CONCLUDING REMARKS .....	125

## INTRODUCTION

Spatial and temporal organization of cellular matter determines the regulation and control of key cellular processes that lead to nontrivial outcomes such as cell division, differentiation, adhesion, motility, stress response, metabolic control, and death (19, 34, 74, 85, 98, 125, 138). Cellular matter can be organized into membrane-bound or membraneless organelles. The latter are biomolecular condensates, which are defined as concentrated nonstoichiometric assemblies of biomolecules (12), that can form via spontaneous or driven processes sharing many of the hallmarks of phase transitions (17, 154).

In 1995, Walter & Brooks (168) proposed that microcompartmentalization, which refers to the spatial organization of cellular matter, might arise due to phase separation mediated by macromolecular crowding in the cytoplasm. A generalization of this idea reemerged following the work of Brangwynne et al. (29), who showed that P-granules in germ cells form via phase separation. Since then, there has been a surge of interest in the phenomenon of liquid-liquid phase separation (LLPS), whereby biomolecular condensates form by spontaneous or driven phase separation of macromolecular components from their liquid-like environments into distinct condensates with liquid-like properties (1-11, 14, 17, 18, 20, 21, 23-25, 27, 28, 30-32, 36, 37, 39, 40, 44, 46-52, 54, 55, 57, 60-63, 67-69, 71, 72, 77-80, 83, 84, 86-90, 92, 93, 95-97, 100-102, 104, 106-109, 111-121, 123, 126, 127, 130, 133, 135-137, 139, 145, 146, 149, 150, 152, 153, 155, 157, 159-162, 164, 169-177, 179, 180, 182-184, 186) (**Figure 1**). The resulting condensates, enriched in specific macromolecules, coexist with the surrounding milieu, which is relatively deficient in the macromolecules of interest. Indeed, there is growing consensus that many membraneless biomolecular



**Figure 1**

Overview of cellular bodies that are well described as biomolecular condensates. These bodies include large, well-studied structures such as the nucleolus, nuclear speckles, and P-bodies, but also smaller assemblies including signalling granules, receptor clusters, and DNA damage foci. The sizes of assemblies in this schematic are not to scale.

condensates form via some combination of spontaneous or driven phase separation and percolation (17, 76). Specific types of protein and RNA molecules drive intracellular phase transitions, and a defining characteristic of these molecules is the multivalence of interaction domains or motifs (12).

Phase separation, especially LLPS, is described using an assortment of analogies to observations made in everyday life. In a two-component system comprising liquids such as oil and water, phase separation is a demixing process whereby two mutually immiscible liquids form two distinct coexisting phases. Alternatively, a mixture comprising a water-soluble polymer in an aqueous solvent can separate into a dense polymer-rich phase that coexists with a dilute, polymer-deficient phase. In two-component systems comprising polymer and solvent, we use  $\phi_p$  and  $\phi_s$  to denote the volume fractions of polymer and solvent, respectively. If the system is closed, then  $\phi_p + \phi_s = 1$ , and it follows that  $\phi_s = (1 - \phi_p)$ ; accordingly, if we set  $\phi_p$  to be  $\phi$ , then the volume fraction of the polymer becomes the order parameter for describing phase separation. Because the system is closed,  $\phi$  is referred to as a conserved order parameter.

### Concepts of Solvent Quality and Findings from Mean-Field Theories

In a binary mixture comprising a polymer and poor solvent, there exists a system-specific concentration threshold designated as the saturation concentration or  $\phi_{\text{sat}}$  (31, 38, 124) beyond which the system separates into a dense polymer-rich phase that coexists with a dilute phase. The volume fractions of the polymer in the coexisting dense and dilute phases are designated as  $\phi_{\text{dilute}}$  and  $\phi_{\text{dense}}$ , respectively, where  $\phi_{\text{dilute}} = \phi_{\text{sat}}$ . For  $\phi_{\text{dilute}} < \phi < \phi_{\text{dense}}$ , the numbers of the polymer molecules in the two phases are determined by the so-called lever rule:  $n_{\text{dilute}} = n_{\text{total}} (\phi_{\text{dense}} - \phi) / (\phi_{\text{dense}} - \phi_{\text{dilute}})$  and  $n_{\text{dense}} = n_{\text{total}} (\phi - \phi_{\text{dilute}}) / (\phi_{\text{dense}} - \phi_{\text{dilute}})$ , where  $n_{\text{dilute}}$  and  $n_{\text{dense}}$  are, respectively, the numbers of polymer molecules in the dilute and dense phases, and  $n_{\text{total}}$  is the total number of polymer molecules:  $n_{\text{total}} = n_{\text{dilute}} + n_{\text{dense}}$  (142).

In mean-field theories for homopolymer solutions, the length ( $N$ ) of the polymer and the magnitude of the Flory interaction parameter  $\chi_{\text{ps}}$ , which is positive in a poor solvent (59), will

determine the values of  $\phi_{\text{dense}}$  and  $\phi_{\text{dilute}}$ . The parameter  $\chi_{\text{ps}}$  is defined as

$$\chi_{\text{ps}} = \frac{z(2u_{\text{ps}} - u_{\text{pp}} - u_{\text{ss}})}{2k_B T}. \quad 1.$$

In Equation 1, the terms  $u_{\text{xy}}$  refer to mean-field energies for interactions between species  $x$  and  $y$ ; the subscripts  $p$  and  $s$  refer to the polymer and solvent, respectively. The algebraic sum of energies is made dimensionless by normalization using the parameter  $k_B T$ , which quantifies the thermal energy at temperature  $T$ ;  $z$  is a coordination number that represents the average number of nearest-neighbor interactions that each monomeric unit within the polymer can make.

In a good solvent,  $\chi_{\text{ps}}$  is negative, implying that polymer–solvent interactions are favored over polymer–polymer interactions. As a result, a homogeneous, one-phase mixture is preferred, irrespective of the value of  $\phi$ . Conversely,  $\chi_{\text{ps}}$  is positive in a poor solvent, reflecting the fact that polymer–polymer interactions are favored over polymer–solvent interactions. In a poor solvent, there exists a  $\chi_{\text{ps}}$ -dependent threshold value of  $\phi$  beyond which the system separates into two coexisting phases; this threshold value is designated as  $\phi_{\text{sat}}$ . In a theta solvent, also known as an indifferent solvent,  $\chi_{\text{ps}} = 0$ , and the polymer–solvent, polymer–polymer, and solvent–solvent interactions are perfectly counterbalanced. Accordingly, the entropy of mixing is the only relevant term, and this favors the formation of an ideal, one-phase mixture in a theta solvent.

For closed multicomponent systems that comprise  $n$  types of homopolymers plus a solvent, the relevant conserved order parameter is a vector denoted as  $[\phi_1, \phi_2, \dots, \phi_n]$ ; in this case,  $\phi_i$  denotes the volume fraction of the polymer of type  $i$ . In a closed system, the volume fraction of the solvent is readily calculated using  $\phi_s = 1 - \sum_{i=1}^n \phi_i$ . For fixed temperature and pressure, the Gibbs phase rule prescribes that there can be a maximum of  $n + 1$  coexisting phases. The determinants of the phase behavior of mixtures comprising multiple types of homopolymers plus a solvent are components of the vector  $\bar{\chi} = [\chi_{12}, \chi_{13}, \dots, \chi_{1s}, \chi_{23}, \dots, \chi_{ns}]$ , where each  $\chi_{ij}$  is defined as in Equation 1; the numeric subscripts correspond to the identities of polymers, and the subscript  $s$  denotes the solvent. The main upshot is that, for aqueous mixtures of homopolymers, the mapping of phase boundaries will require knowledge of the components of the vector  $\bar{\chi}$  through either numerical calculations or suitable measurements (99).

The above discussion is inspired by the influential theories of Flory and Huggins (for a discussion, see 142), and it relies on a purely mean-field description for homopolymers. The vector  $\bar{\chi}$  contains all of the information that is relevant for describing the driving forces for phase separation. It is a measure of solvent quality and the mutual (in)compatibilities of polymers with one another. The compositions of dense phases and the interfacial tensions between pairs of coexisting phases are determined directly by the values of the components in the vector  $\bar{\chi}$ . For homopolymers, all interactions are equivalent, and  $\bar{\chi}$  can be used to capture the interplay of polymer and solvent interactions to describe phase behavior.

## Going Beyond Homopolymers

Homopolymers are poor approximations of most of the protein and RNA molecules that are drivers of intracellular phase transitions. These molecules are finite-sized heteropolymers of precise molecular weights that comprise structured domains and motifs, intrinsically disordered regions (IDRs), or some combination of the two. The vector  $\bar{\chi}$  captures neither the sequence and structural heterogeneities nor the hierarchy of anisotropic interactions encoded by the multiway interplay among heteropolymers and the solvent. Therefore, motivated by modern developments in polymer theories, we propose that protein and RNA molecules that drive intracellular phase transitions are in fact biological instantiations of associative polymers, which were defined by

Rubinstein & Dobrynin (143, p. 181) to be “macromolecules with attractive groups.” The attractive groups are distributed across the polymer. Furthermore, the interactions involving these groups can be anisotropic; these interactions include ionic bonds, hydrogen bonds, and interactions mediated by solvents known as gluonic and regulatory solvents (156).

In much the same way that the Flory-Huggins theory provides a general framework for describing homopolymeric systems, associative polymers can be described using a stickers-and-spacers model, where the mean-field free energy term from the Flory-Huggins theory is augmented by specific interactions among stickers. The groups that participate in attractive interactions are considered to be stickers, and the parts of the chain that are interspersed between stickers but do not significantly drive attractive interactions are considered to be spacers. Noncovalent interactions between stickers within and from different chains will lead to the formation of reversible physical crosslinks (143). Although spacers are not directly involved in these crosslinks, they can have a profound impact on the assembly of associative polymers.

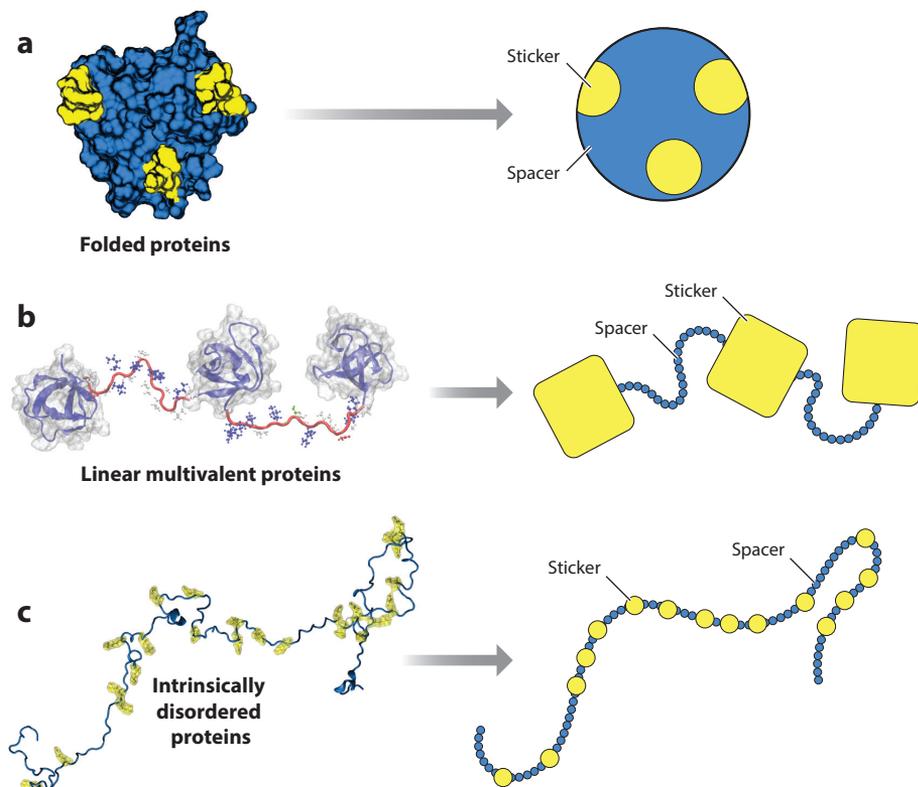
Multivalent protein and RNA molecules may be either branched or linear associative polymers. Therefore, an important question in applying the stickers-and-spacers model to biopolymers pertains to the molecular identities of stickers. In IDRs, stickers are likely to be short linear motifs (SLiMs) that are 1–10 residues in length, while spacers are the intervening residues in the IDR (43). Analogously, in unfolded RNA molecules, stickers may be short sequence motifs or even individual nucleotides. Stickers in folded protein domains or structured regions of RNA are surface patches or motifs that emerge from the formation of specific structures. Accordingly, non-sticker regions on the surfaces of folded domains of proteins and disordered loop regions can be considered as spacers. In linear multivalent systems, stickers may be folded binding domains, while spacers are the flexible disordered linkers that connect them together. For branched multivalent proteins, disordered regions give these systems a hairy colloidal architecture, and the disordered regions, sans the SLiMs, may be thought of as spacers. **Figure 2** shows a schematic of different types of multivalent protein and RNA molecules that are mapped onto sticker-and-spacer architectures.

Importantly, the stickers-and-spacers model does not have restrictions on either the identity of stickers or the resolution at which stickers are defined. Accordingly, the stickers-and-spacers model offers an intuitive and highly generalizable approach for quantitative descriptions of complex biological systems. In the following sections, we discuss key details of the stickers-and-spacers formalism for obtaining a thermodynamic description of the phase behavior of associative polymers in solution. We summarize predictions that can be made using this model, cite numerical instantiations of the model, and highlight applications to specific protein and RNA systems.

## MEAN-FIELD INCARNATION OF THE STICKERS-AND-SPACERS MODEL

One possible quantitative realization of the stickers-and-spacers framework is an analytical mean-field model for associative polymers. This model rests on the simplifying assumption that the conformational preferences of individual associative polymers are similar in their dense versus dilute phases. This simplification allows us to ignore the possibility that conformational changes might lead to changes in the valence and identities of stickers.

We consider a two-component system comprising associative polymers with multiple interacting stickers interspersed by noninteracting phantom spacers. The model for spacers assumes that the interactions involving spacers (i.e., sticker-spacer, spacer-spacer, and spacer-solvent) counterbalance one another, thus making the spacer regions behave like an ideal chain. Physical crosslinks between stickers enable two types of transitions. Aided by the nature of spacers, the physical crosslinks among stickers can lead to a density transition (which is phase separation) whereby,



**Figure 2**

Schematic of different types of stickers and spacers for different systems. (a) For folded domains, the mapping of the stickers and spacers is achieved via the physics of patchy colloids, whereby the stickers are the interaction patches and the spacers are regions on the globular domain that serve as the surface scaffold for stickers. (b) For linear multivalent proteins, we can broadly map stickers as folded binding domains, while spacers are flexible linkers that connect domains. This does not rule out the prospect that disordered regions also comprise either primary or auxiliary stickers. (c) For intrinsically disordered proteins, stickers may be single residues, short linear motifs, or some combination of the two.

above a threshold concentration denoted as  $c_{\text{sat}}$ , the associative polymers in a binary mixture comprising the polymers and solvent will form a dense phase defined by physically crosslinked stickers that coexists with a dilute phase comprising minimal inter-sticker crosslinks. The concentrations of associative polymers or stickers in the coexisting dilute and dense phases are denoted, respectively, as  $c_{\text{dilute}} = c_{\text{sat}}$  and  $c_{\text{dense}}$ . Associative polymers also undergo a networking transition known as percolation. This is governed by the topological connectivity among stickers that is engendered by physical crosslinks. Above a concentration threshold  $c_{\text{perc}}$ , known as the gel point or percolation threshold, the system of associative polymers can form a system-spanning network. Phase separation leads to percolation if  $c_{\text{sat}} \leq c_{\text{perc}} < c_{\text{dense}}$ . Conversely, phase separation and percolation become decoupled from one another if  $c_{\text{dense}} < c_{\text{perc}}$  (phase separation without percolation) or  $c_{\text{perc}} < c_{\text{sat}}$  (percolation without phase separation). For the purpose of developing the mean-field theory, we assume that we are operating in the regime where  $c_{\text{sat}} \leq c_{\text{perc}} < c_{\text{dense}}$ .

For a system comprising associative polymers in a solvent, each with  $n$  self-interacting stickers ( $n \gg 1$ ), Semenov & Rubinstein (151) showed that the percolation threshold for a system in which

stickers are described as phantom chains is estimated as

$$c_{\text{perc}} \approx \frac{1}{\lambda n^2}. \quad 2.$$

In this case,  $n$  is the apparent valence (number) of stickers, and  $\lambda = v_b \exp(-\frac{\epsilon}{k_B T})$ , where  $v_b$  is the volume associated with each inter-sticker crosslink,  $\epsilon$  is the effective interaction energy between stickers ( $\epsilon \leq 0$ ),  $k_B$  is the Boltzmann constant, and  $T$  is the system temperature. We describe the origins of the relationship between  $c_{\text{perc}}$  and the valence of stickers by summarizing the extension of the theory of Semenov & Rubinstein (151) to the case of an associative polymer that consists of two types of stickers, A and B.

### An Obligate Heterotypic-Interaction Model for Stickers and Spacers

The theory of Semenov & Rubinstein (151) was extended by Wang et al. (170) to describe the measured variations of  $c_{\text{sat}}$  with the apparent valence (numbers) of Arg and Tyr residues that are considered to be the main stickers in FUS and FET family proteins. We follow Wang et al. (170) and assume that  $\epsilon_{AA} = \epsilon_{BB} = 0$  and  $\epsilon_{AB} < 0$ . This implies that the effective attractions arise purely from heterotypic interactions among stickers. Since  $\epsilon_{AB} < 0$ , it follows that  $(-\epsilon_{AB}/k_B T) > 0$ ; thus, we write the Boltzmann weight as  $\exp(|\epsilon_{AB}|/k_B T)$ , where the numerator of the exponent refers to the magnitude of the attractive interactions between A and B stickers.

We consider a system comprising  $N$  associative polymers in a solvent, each with  $n_A$  and  $n_B$  stickers of type A and B, respectively. The spacers between the stickers are inert, phantom chains. The free energy of the system is written as

$$\frac{F}{k_B T} = -\ln Z. \quad 3.$$

The partition function  $Z$  can be calculated using the mean-field approach of Semenov & Rubinstein (151) as

$$Z = \Omega \exp\left(\frac{N_{\text{pairs}} |\epsilon_{AB}|}{k_B T}\right) \left(\frac{v_b}{V}\right)^{N_{\text{pairs}}}. \quad 4.$$

In Equation 4,  $\Omega$  is a combinatorial factor,  $N_{\text{pairs}}$  is the total number of extant pairs of A–B crosslinks in the system,  $v_b$  is the bond volume associated with each physical crosslink, and  $v$  is the system volume. The combinatorial factor is computed as

$$\Omega = \binom{N n_A}{N_{\text{pairs}}} \binom{N n_B}{N_{\text{pairs}}} N_{\text{pairs}}!. \quad 5.$$

Substitution of Equation 5 into Equations 4 and 3 leads to

$$\begin{aligned} \frac{F}{k_B T} = & -N n_A \ln(N n_A) + (N n_A - N_{\text{pairs}}) \ln(N n_A - N_{\text{pairs}}) \\ & -N n_B \ln(N n_B) + (N n_B - N_{\text{pairs}}) \ln(N n_B - N_{\text{pairs}}) \\ & + N_{\text{pairs}} \ln\left(\frac{N_{\text{pairs}} V}{v_b}\right) - \left(\frac{|\epsilon_{AB}|}{k_B T} - 1\right) N_{\text{pairs}}. \end{aligned} \quad 6.$$

Minimizing this free energy with respect to  $N_{\text{pairs}}$  leads to

$$\frac{(N n_A - N_{\text{pairs}})(N n_B - N_{\text{pairs}})}{N_{\text{pairs}}} = \frac{V}{\lambda}. \quad 7.$$

In this case, the attractive volume is  $\lambda = v_b \exp(\frac{\epsilon_{AB}}{k_B T})$ . Solving the quadratic equation yields the following expression for  $N_{\text{pairs}}$  that minimizes  $F$ :

$$N_{\text{pairs}} = \frac{1}{2} \left[ Nn_A + Nn_B + \frac{V}{\lambda} - \sqrt{\left( Nn_A + Nn_B + \frac{V}{\lambda} \right)^2 - 4N^2 n_A n_B} \right]. \quad 8.$$

A total of  $N_{\text{pairs}}$  stickers of type A and  $N_{\text{pairs}}$  stickers of type B will participate in  $N_{\text{pairs}}$  crosslinks. Accordingly, the fraction of interacting stickers (or crosslinks) in each chain will be

$$p = \frac{2N_{\text{pairs}}}{N(n_A + n_B)}. \quad 9.$$

Replacing  $N_{\text{pairs}}$  in Equation 8 with  $p$  leads to

$$p = \frac{1}{n_A + n_B} \left[ n_A + n_B + \frac{1}{\lambda c} - \sqrt{\left( n_A + n_B + \frac{1}{\lambda c} \right)^2 - 4n_A n_B} \right]. \quad 10.$$

In this case,  $c$  is the polymer concentration  $N/v$ . If we set the strengths of sticker-sticker interactions such that  $\lambda c \ll 1$  (weak interactions), then

$$p \approx \frac{2\lambda c n_A n_B}{n_A + n_B}. \quad 11.$$

Based on the Flory-Stockmayer theory (58, 158), we know that, at the percolation threshold  $c_{\text{perc}}$ , the value of  $p$  designated as  $p_{\text{perc}}$  is

$$p_{\text{perc}} = \frac{1}{n_A + n_B + 1}. \quad 12.$$

Substituting Equation 12 into the left-hand side of Equation 11 and setting  $c = c_{\text{perc}}$  on the right-hand side of Equation 11 leads to the following estimate for  $c_{\text{perc}}$ , which is valid for  $n_A + n_B \gg 1$ :

$$c_{\text{perc}} = \frac{1}{2\lambda n_A n_B} \left( \frac{n_A + n_B}{n_A + n_B - 1} \right) \approx \frac{1}{2\lambda n_A n_B} \sim \frac{1}{n_A n_B}. \quad 13.$$

### Extending the Obligat Heterotypic Model to Include Homotypic Sticker Interactions

Using a similar extension of the mean-field model developed by Prusty et al. (134), who applied the model to a system comprising distinct polymers with A and B stickers, one can include the effects of homotypic sticker attractions by setting  $\epsilon_{AA} \neq 0$  and  $\epsilon_{BB} \neq 0$ . In this scenario, a generalization of the approach detailed above leads to the following expression for the percolation threshold:

$$c_{\text{perc}} \sim \frac{1}{\lambda_{AA} n_A^2 + 2\lambda_{AB} n_A n_B + \lambda_{BB} n_B^2}. \quad 14.$$

In Equation 14,  $\lambda_{ij}$  is the attractive volume for the  $i$ - $j$  interaction, i.e.,  $\lambda_{ij} = v_{ij} \exp(\frac{|\epsilon_{ij}|}{k_B T})$ , where  $\epsilon_{ij} \leq 0$  is the interaction energy, and  $v_{ij}$  is the bond volume for the  $i$ - $j$  interaction. Note that Equation 14 reduces to the expression in Equation 13 if the effects of homotypic interactions between stickers are ignored.

## What if We Have Multiple Types of Stickers in Our System?

The model can be further generalized to a system comprising polymers with more than two types of stickers. The percolation threshold is estimated using Equation 15, written as

$$c_{\text{perc}} \sim \frac{1}{\sum_i \lambda_{ii} n_i^2 + 2 \sum_{i \neq j} \lambda_{ij} n_i n_j}. \quad 15.$$

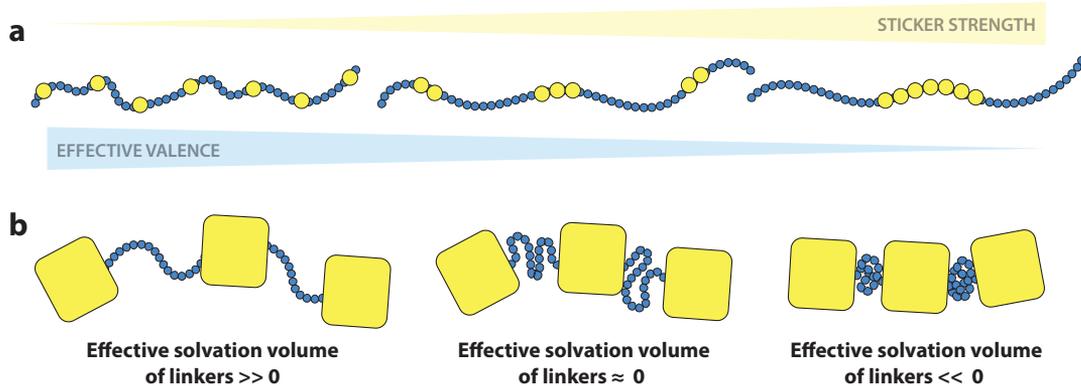
In this case,  $i$  and  $j$  are sticker type indices,  $\lambda_{ij}$  is the attractive volume for the  $i$ - $j$  interaction, and  $n_i$  is the number of stickers of type  $i$  in each polymer. As shown in Equation 15, the contribution of each sticker pair interaction is additive, weighted by the attractive volume  $\lambda_{ij}$ . Thus, if a certain  $\lambda_{pq}$  term is much greater than other terms such that the percolation concentration can be approximately evaluated by only considering  $\lambda_{pq} n_p n_q$ , then we can consider only stickers  $p$  and  $q$  as relevant stickers, and other stickers can be considered as spacers. This implies that there is no fixed set of stickers, and a set of stickers in one system can play the role of spacers in another system, depending on the relative contributions of different stickers to the percolation threshold.

## Effects of Spacers

The preceding section builds on the work of Semenov & Rubinstein (151) and prescribes a quantitative, albeit mean-field, model for quantifying the effects of stickers on the driving forces for phase separation and percolation. One can also use the percolation threshold as a suitable proxy for estimating the saturation concentration for phase separation, providing  $c_{\text{sat}} \leq c_{\text{perc}} < c_{\text{dense}}$ . Whether this condition is satisfied will be determined by the nature of the spacers.

The mean-field model introduced above treats spacers as phantom chains. A simple way to account for the effects of spacers is to include ad hoc spacer-specific corrections to the average volume per crosslink, i.e., the value of  $v_b$ . However, for realistic scenarios, one has to account explicitly for the effects of spacers. There are three possible effects of spacers that one must consider: (a) the excluded volumes (also referred to as the effective solvation volumes) of spacers (66), which can be included using the standard Flory-Huggins formalism; (b) the contribution of auxiliary attractions between sites along spacers and specific stickers; and (c) attractive interactions between spacers that, by the definition of spacers, will be weaker than sticker-sticker interactions. In the limit of strong attractions among spacers, associative polymers essentially become akin to homopolymers in poor solvents, and the distinction between a stickers-and-spacers framework and a homopolymer model becomes minimal because all of the entities are equivalent to one another. Strong (*vis-à-vis*  $k_B T$ ) sticker-sticker, sticker-spacer, and spacer-spacer interactions will drive aggregation and/or precipitation into amorphous or fibrillar solids. These assemblies are distinct from the fluid-like phases that would be formed by associative polymers. Accordingly, the excluded volumes generated by spacers and their relatively weak auxiliary interactions with stickers are the main contributions that spacers make to the phase behavior of associative polymers.

The excluded volume ( $v_{\text{ex}}$ ), also referred to as the effective solvation volume ( $v_{\text{es}}$ ), is the average volume per spacer site that is set aside for interactions with the surrounding volume (142) (**Figure 3b**). It is governed by the effective, solvent-mediated, pairwise interactions between spacer sites. If these interactions are net attractive, then  $v_{\text{ex}}$  is negative, implying that the spacer sites sequester themselves from the surrounding solvent, giving rise to compact spacers. Conversely, if the effective interactions are repulsive, then  $v_{\text{ex}}$  is positive, implying that the spacer sites interact preferentially with the surrounding solvent, thereby giving rise to spacers that are conformationally expanded. If the spacer-solvent, solvent-solvent, and spacer-spacer interactions counterbalance one another, then  $v_{\text{ex}} \approx 0$ , implying that spacers behave like ideal chains. In theory, this



**Figure 3**

Schematic of sticker patterning and effective solvation volume. (a) Three distinct sequences of intrinsically disordered proteins with identical numbers of sticker residues distributed in different arrangements. As sticker residues are clustered together, the effective sticker identity may change such that, as the number of stickers decreases, the strength of each individual sticker increases. (b) Physical manifestation of the effective solvation volume (also known as the excluded volume) for linkers. A positive effective solvation volume is associated with expanded linkers, while a negative effective solvation volume leads to a collapsed and self-interacting linker. An effective solvation volume of zero derives from sequence features that give rise to counterbalanced linker–linker and linker–solvent interactions, thus engendering ideal chain behavior for the linkers.

should reproduce the mean-field behavior described above, since the mean-field model is based on so-called phantom spacers. However, the spacers with zero excluded volume can enhance the sticker–sticker interactions, and this cooperative effect leads to phase separation being realized at concentrations that are well below the percolation threshold that would be predicted based on the Flory-Stockmayer theory; this is because the Flory-Stockmayer theory only considers the valence of stickers and the bond formation probability and ignores the intrinsic connectivity due to spacers (58, 158).

Harmon et al. (66) performed lattice-based simulations intended to mimic the poly-SH3 and poly-PRM systems studied by Rosen and coworkers (15, 16, 87). Simulations showed that spacers mimicking self-avoiding walks have high positive excluded volumes, and the preferential interactions of these spacers with solvent will inhibit the cooperative interactions that are required to drive phase separation. Instead, the high excluded volumes lead to an upshift in the calculated percolation threshold when compared to expectations from the Flory-Stockmayer limit (58, 158). For associative polymers with high positive excluded volume spacers, percolation occurs above a percolation threshold, but this is realized without phase separation, implying that  $c_{\text{perc}} > c_{\text{sat}}$  for such systems. As the spacer excluded volumes decrease, there is a stronger coupling between phase separation and percolation; this implies that the low excluded volumes of spacers enable cooperative interactions among spacers that, in turn, enable concomitant density and percolation transitions.

To account theoretically for the effects of spacers that were quantified in simulations, one has to be able to calculate the signs and magnitudes of excluded volumes for each of the spacer regions. This will allow the incorporation of suitable corrections or higher-order terms due to spacer contributions into quantitative models that allow one to predict  $c_{\text{sat}}$ ,  $c_{\text{perc}}$ , and  $c_{\text{dense}}$  directly from the sequence. Continued integration between theory and simulation should permit the development of a comprehensive model that accounts for sticker valence, sticker interaction strengths, spacer excluded volumes, and higher-order contributions to interactions among associative polymers that are due to auxiliary attractive interactions between spacer sites and specific stickers.

## IDENTIFYING STICKERS VERSUS SPACERS

The identification of stickers can be performed computationally and/or experimentally. As a rule of thumb, the loss of a sticker should have a substantial impact on  $c_{\text{sat}}$ , while the loss of a spacer should have minimal effects on  $c_{\text{sat}}$ . Alternatively, for multicomponent systems where the concentrations of the coexisting dilute and dense phases are not fixed quantities (see 35, figure 12), thus generalizing the concept of a saturation concentration, the rule of thumb generalizes to asking whether the loss of a sticker alters the location and slope of the coexistence curve. These are simple albeit useful zeroth-order distinctions, but quantitatively, what constitutes a substantial impact will vary across systems. A brute-force approach to identifying stickers versus spacers would be full mutagenesis of every residue using alanine or glycine scanning and/or saturation mutagenesis that is coupled with the measurements of  $c_{\text{sat}}$  for binary mixtures and/or full coexistence curves for multicomponent systems comprising each mutant. This would provide a systematic assessment of the contribution that each residue makes to the saturation concentration and/or coexistence curve, allowing those that contribute substantially to be delineated as stickers (or as falling within sticker motifs), while those that do not are delineated as spacers. In contrast, we can perform a systematic mutation of specific residues of interest, identified a priori using bioinformatics approaches (122, 166, 167, 178), to all possible amino acids. This directed saturation mutagenesis allows a direct comparison between two positions across equivalent sequence changes.

### Spectroscopic Routes to Identifying Stickers Versus Spacers

Rather than assessing the functional consequence of loss (or gain) of stickers, an alternative approach is the biophysical dissection of sticker-mediated intermolecular interactions. Instead of measuring  $c_{\text{sat}}$  and/or full coexistence curves, the early stages of assembly and/or deviations from ideal solution behavior can be measured using various methods, including light scattering and fluorescence correlation spectroscopy (FCS). As an example, measuring the second virial coefficient ( $B_2$ ) using laser light scattering and/or osmotic pressure measurements as a function of sequence perturbation and changes to solution conditions provides one route to dissect how distinct residues or motifs contribute to intermolecular interaction (128).

Nuclear magnetic resonance (NMR) spectroscopy is also a powerful experimental technique that provides the requisite site-specific information that can be used to identify stickers versus spacers (16, 20, 27, 164). For IDRs, transverse relaxation rates ( $R_2$ ) provide information regarding local dynamics, and these may be slowed for stickers engaging in interactions with one another (105, 147). Chemical shift perturbations measured as functions of protein concentration can also provide insight into intermolecular interactions, as can cross-saturation transfer experiments. If appropriately designed experiments are performed, then paramagnetic relaxation enhancement mediated by spin labels provides an alternative approach to assess transient intermolecular interactions. Finally, if sufficiently strong intersticker interactions are present, then it may be possible to detect these using intermolecular nuclear Overhauser effects.

Many approaches used to identify stickers versus spacers will depend on the architecture of the protein and RNA molecules of interest. We define three common classes of biopolymers that fit the stickers and spacers architecture: folded domains, linear multivalent systems, and IDRs (**Figure 2**). Folded domains may be thought of as being analogous to rigid or deformable patchy colloids (117). Accordingly, the goal is to identify the attractive patches (stickers) on the surfaces of folded domains, the range and directionality of their attractions, any fluctuations associated with folded domains that may account for fluctuations between sticker-sticker interactions, and the nature of any spacer-mediated auxiliary interactions (178). A combination of computational, theoretical, and experimental approaches that have been deployed in the context of studying

the phase behavior of proteins that undergo crystallization can be adapted to identify stickers versus spacers for folded domains and quantify the interaction strengths among stickers and spacers.

The term linear multivalent proteins refers to polypeptides in which multiple folded domains are connected by flexible linker IDRs (66). Examples of such a system are the poly-SH3 + poly-PRM and the poly-SUMO + poly-SIM systems (13). For systems in which folded domains are well-defined binding modules, the stickers are readily identified as binding sites on the interaction domains (SH3 or SUMO) and their cognate partners (PRM or SIM). The relative importance of specific residues in these binding sites can be assessed by mutational studies, but auxiliary interactions mediated by residues distal from these sites may also have a modulatory role (16). In these types of modular systems, the flexible linkers that connect folded domains can be viewed as the spacers. The surface residues that lie outside the binding sites may also be viewed as auxiliary spacers. Similar approaches can be applied to branched multivalent proteins comprising folded oligomerization domains and IDRs, as in the case of nucleophosmin 1 (NPM1) (57), or even oligomeric proteins such as metabolic enzymes that are devoid of IDRs.

To identify and delineate stickers from spacers within IDRs, we can take advantage of the maturity of methods that are now routinely being brought to bear on the analysis of conformational ensembles of disordered proteins in dilute solutions. This becomes an informative exercise in the context of IDRs that lack persistent secondary or tertiary structural preferences, as there is an intrinsic equivalence between intermolecular and intramolecular interactions. Degenerate interactions, in the form of a network of intramolecular physical crosslinks among stickers along an IDR, can lead to the partial collapse of individual molecules. Two distinct types of parameters can be determined from these single-chain simulations: parameters determined from the sequence alone and the apparent valences of stickers and chain length. Additionally, one can obtain parameters that are governed by a combination of sequence and solution conditions and include the sticker-sticker interaction strengths and the excluded volumes of spacer regions. Both sets of parameters play a key role in determining the extent of collapse of an individual disordered protein in dilute solutions and, consequently, the extent of intermolecular interactions in sufficiently concentrated solutions. Accordingly, an assortment of methods that combine experimental and computational approaches can be used to identify and delineate stickers versus spacers in IDRs.

The combination of methods described for multivalent proteins can also be brought to bear on identifying stickers versus spacers in RNA molecules. These methods can be augmented by RNA structure prediction methods that help identify regions of complementarity that are likely to be involved in making secondary structures via base pairing and base stacking. Secondary and tertiary structure predictions are readily tested using methods such as selective 2'-hydroxyl acylation analyzed by primer extension (94) that are sensitive to the presence of specific types of structural motifs. Recent work has shown that the ratio of purines to pyrimidines is an important determinant of the driving forces for phase separation in disordered RNA molecules (22). This observation provides a useful heuristic to quantify comparative driving forces for phase separation on the basis of the apparent valence of purine-based stickers compared to pyrimidine-based spacers.

### Apparent Valence Versus Effective Valence of Stickers

The approaches of Semenov & Rubinstein (151) focus primarily on the apparent valence of stickers. Recent studies have shown that the clustering and segregation of stickers along linear sequences can have a profound effect on the driving forces for phase separation. For a fixed number (apparent valence) of stickers, sequence patterning can increase or decrease the effective valence of

stickers (**Figure 3a**). Coarse-grained simulations based on transferrable (46), phenomenological (35, 57), or learned models (144) have been developed and deployed to study the phase behavior of an assortment of protein and RNA molecules that include a combination of folded domains and disordered regions (65, 66, 131, 141). The results of simulations can be analyzed using mean-field theories, and discrepancies between theoretical predictions and computational results can be used to extract the effective valence of stickers, thereby going beyond the apparent valence extracted from sequence analysis alone.

An important theoretical advance that accounts for sequence patterning effects, specifically the clustering versus segregation of charged residues, comes from Chan and coworkers (91, 92). Building on observations of the contributions of charge patterning to the dimensions of disordered proteins, Lin & Chan (91) adapted the generalized random phase approximation originally introduced by Ermoshkin & Olvera de la Cruz (53) for synthetic polymers to incorporate sequence correlations among charged stickers and a mean-field correction to model cation- $\pi$  interactions. Their model has been used to predict differences in phase behavior for sequences that have identical numbers (apparent valence) of charged residues but are distinguished by the patterning of oppositely charged residues along the linear sequence (27). Their predictions reveal that the effective valence is lower than the apparent valence for sequences where the oppositely charged residues are segregated along the linear sequence, but the strength of sticker-sticker interactions increases substantially when compared to sequences with a more uniform distribution of charged stickers. In contrast, the effective valence is lower than the apparent valence for sequences where the oppositely charged residues are well mixed along the linear sequence. The predictions of Chan and coworkers have also been borne out in orthogonal field-theoretic simulations and in experiments based on synthetic polymers (103). These studies, as well as in vitro and in cell experiments aided by sequence design approaches (123), highlight the importance of sequence patterning effects as determinants of the effective valence as opposed to the apparent valence.

The apparent and effective valences can also deviate from one another if the associative polymer of interest is characterized by conformational heterogeneity. For highly structured systems and maximally disordered systems, there is likely to be a one-to-one correspondence between apparent valence and effective valence. Between these limiting scenarios, the dominant conformations in the ensembles within dilute and coexisting dense phases will govern the effective valence.

## **CONTRIBUTIONS OF STICKER-STICKER CROSSLINKS AND SPACER EXCLUDED VOLUMES TO STRUCTURAL AND DYNAMICAL PROPERTIES OF CONDENSATES**

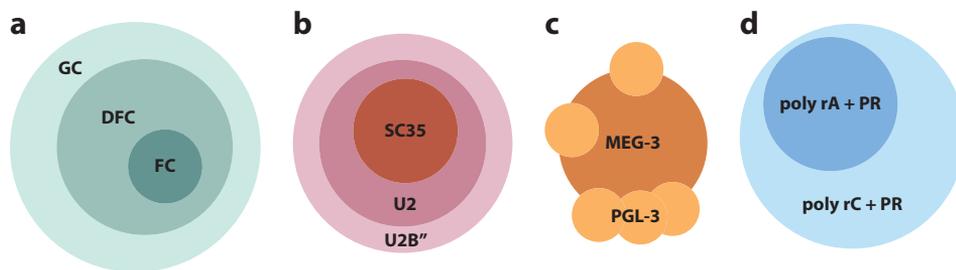
Condensates formed by associative polymers are not simple liquids, which are formed by spherical molecules with isotropic interactions. In contrast, liquids formed by associative polymers are characterized by physical crosslinks among highly flexible (disordered) polymers or patchy colloidal (ordered) molecules. Accordingly, these liquids are best described as network fluids (45).

The rheological properties of network fluids are governed by the extent of crosslinking, the timescales associated with making and breaking of physical crosslinks, the concentration of stickers within the dense phase, and the modulatory impact of spacers (45). Network fluids are not purely viscous liquids, but they behave like elastic materials on timescales shorter than the lifetimes of crosslinks (143). On longer timescales, these fluids behave like viscous materials, and therefore, network fluids are in fact viscoelastic rather than purely viscous fluids. Rheological characterization of viscoelastic materials requires the measurement of dynamic moduli, which quantifies the ratio of stress to strain of the fluid under the influence of oscillatory forces (141, 143). Of direct

relevance is the response of a network fluid to shear stresses and strains. If the fluid is purely viscous, then the shear strain, which refers to the deformation of the network, will lag behind the shear stress, which refers to the breaking of the network. Conversely, in a purely elastic material, the stress and strain are perfectly in phase. The phase angle between stress and strain can be quantified in terms of the dynamic modulus  $G^*$ , which is a complex variable written as  $G^* = G' + iG''$ . In this case,  $G'$  and  $G''$  are the shear storage and shear loss moduli, respectively. The storage modulus quantifies the energy stored in the network and is determined by the extent of physical crosslinking and the strengths of the crosslinks. In contrast, the loss modulus quantifies the extent of energy dissipation and is governed by the viscosity of the fluid. Values of storage and loss moduli can be measured as functions of shearing frequency, and the phase angle  $\delta$  is calculated as the ratio of loss to storage modulus, i.e.,  $\tan \delta = (G''/G')$ .

### Is the Distinction Between Viscous and Viscoelastic Network Fluids Relevant or of Functional Importance?

Nucleoli (57), nuclear speckles (56), P-granules (73, 135), and even very simple synthetic condensates (22, 155) show characteristics of multilayered, multicomponent behavior (**Figure 4**). Distinct layers are likely to form via different molecular interaction networks, and these may lead to different viscoelastic behaviors. Rheological measurements show that the fibrillar-rich dense fibrillar center (DFC) of nucleoli derived from oocytes is a bona fide viscoelastic material (57). Comparatively, the NPM1-rich granular component appears to be more of a viscous material than the DFC. Nucleoli and nuclear speckles appear to have similar organizations in that their cores are more viscoelastic than the outer layers, which are more viscous. This type of architecture might have a bearing on where and when rRNA and ribosomal proteins, which experience opposing radial fluxes in nucleoli, will encounter one another and undergo ribosomal assembly (109). In contrast to nucleoli and nuclear speckles, condensates formed by essential P-granule components such as MEG proteins and their cognate RNA molecules appear to have viscous cores surrounded by viscoelastic shells (135). Although rheological measurements are not available for this condensate, inferences were drawn using data from experiments based on fluorescence recovery after photobleaching, and these might come with requisite caveats regarding their analyses (163). The coexistence with viscous protein-like liquids and apparently viscoelastic materials comprising physically crosslinked



**Figure 4**

Four examples of multiphase assemblies formed for different multicomponent systems. (a) Three-phase assembly of nucleoli is readily reproduced using a simple stickers-and-spacers model, as shown by Feric et al. (57). (b) Distinct types of nuclear speckle architecture can also be recapitulated in a similar manner, as shown by Fei et al. (56). (c) MEG-3 and PGL-3 form distinct phases in P-granules and in vitro, as demonstrated by Putnam et al. (135). (d) A simple four-component system (solvent, proline–arginine dipeptides, polyadenosine, polycytosine) forms two distinct dense phases due to distinct sticker–sticker strengths, as described by Boeynaems et al. (22).

RNA molecules is also readily observed in binary and ternary systems with simple dipeptide-rich proteins and homopolymeric RNA molecules (22).

### Connecting Dynamic Moduli to Internal Structures Within Condensates

Dynamic moduli quantify the material properties of viscoelastic network fluids, and these moduli are determined by the spatial organization of associative polymers with respect to one another within condensates. Spatial organization of molecules will also determine the crosslinking density within condensates. One can quantify spatial organization using distribution functions, such as pair and triplet distribution functions, that serve as primary descriptors of the structures of liquids. These structural descriptors, which delineate the length scales for short-range spatial order versus long-range disorder, can be augmented by descriptions of orientational distribution functions as well. The use of distribution functions completely revolutionized the studies of simple liquids and molecular fluids formed by small molecules. Building on these advances, Zwanzig & Mountain (185) derived direct connections between the structures of liquids quantified in terms of pair distribution functions and dynamic moduli for simple liquids. Extensions of these approaches to connect structural descriptions of network fluids formed by associative polymers to their dynamic moduli are precisely the types of connections between structural descriptions of condensates and their material properties that are needed to understand structure–function relationships on mesoscales defined by nonstoichiometric macromolecular assemblies. Such efforts will be aided by recent advances in small-angle neutron scattering measurements that enable the measurement of indirect Fourier transforms of pair distribution functions, as has been demonstrated by Mitrea et al. (108) for facsimiles of pentameric NPM1 that form condensates through heterotypic interactions with Arg-rich ligands.

### THE STICKERS-AND-SPACERS MODEL IN BIOLOGICAL SYSTEMS

A variety of condensate-driving systems, including multivalent protein and RNA molecules, appear to conform to the stickers-and-spacers architecture. The earliest demonstration of the relevance of the stickers-and-spacers model was made by Rosen and coworkers (15, 87), who studied the phase behavior of linear multivalent proteins in solution and anchored to membranes. In accord with the predictions of Semenov & Rubinstein (151) and tenets of the Flory-Stockmayer theory, the valence of interaction domains was shown to contribute directly to the driving forces for phase separation and percolation or gelation. Furthermore, in cells, multisite Tyr phosphorylation was shown to regulate the overall valence of stickers by recruiting multiple proteins with multiple SH3 and SH2 domains to the membrane-anchored protein nephrin (87).

Associative polymers can form system-spanning networks, a phenomenon that is known as percolation. If phase separation and percolation are coupled ( $c_{\text{sat}} \leq c_{\text{perc}} < c_{\text{dense}}$ ), then the dense phase is a percolated network. In the scenario where the dense phase is a spherical droplet, it follows that the associative polymer forms a droplet-spanning network that coexists with a dilute phase of non-networked molecules. Associative polymers can also form networked solid phases, as is the case with so-called self-assembled fibrillar networks (42). In these cases, the associative polymers form fibrillar structures—as has been observed with several low-complexity sequences—at sufficiently high concentrations. These fibrils are crosslinked to form networks that are akin to self-supporting hydrogels, and in contrast to systems that undergo LLPS through weak degenerate multivalent interactions, these systems are characterized by the acquisition of specific structural biases within the networked phase that are largely absent from polypeptides in the dilute phase.

In the context of low-complexity intrinsically disordered proteins, McKnight and coworkers (64, 75, 81, 82) identified stickers that drive the formation of cross-beta structures and enable the

networking of fibrils, thus giving rise to highly networked hydrogels. The Eisenberg group leveraged their ability to make microcrystals using peptide fragments to identify stickers that enable the formation of intermolecular crosslinks in the form of hydrogen bonds and zippering interactions. In their parlance, Eisenberg and coworkers (70) refer to the stickers as LARKS (low-complexity aromatic-rich kinked segments) due to their sequence composition and the fact that they form cross-beta structures with a characteristic kinked topology, in contrast to standard amyloid cross-beta regions.

Brangwynne et al. (31) proposed that stickers in disordered regions were likely to be SLiMs made up of charged, polar, and aromatic moieties. Drawing on the decades-old work of Burley & Petsko (33), Brangwynne et al. proposed that the three categories of residues were likely to be involved in a hierarchy of weakly polar interactions due to their intrinsic multipole moments. Charged residues such as Arg are defined by a monopole moment (charge of  $+1e$ ), a finite dipole moment, and a significant quadrupole moment due to the planarity of the guanido group. In contrast, Lys has a spherically symmetric functional group and is better approximated as a point charge with a monopole moment (charge of  $+1e$ ) but a negligible dipole or quadrupole moment. This would imply that Arg would be a superior sticker residue over Lys given the hierarchy of interactions that it encodes. In accord with this expectation, Wang et al. (170) showed that the network of Arg-Tyr interactions derived from the high valence of Arg residues within the RNA binding domain (RBD) and equally high valence of Tyr residues within the prion-like domain (PLD) contributes directly to the driving forces for phase separation of the protein FUS. Mutations of Arg to Lys within the RBD weaken the driving forces by approximately tenfold, as measured by the impact of these mutations on the value of  $c_{\text{sat}}$ . Tyr residues have zero net charge (zero monopole moment) but a large dipole moment, due to the in-plane arrangement of the -OH group with the planar pi system, and a significant quadrupole moment that is in accord with its aromaticity. In contrast, Phe has a near-zero dipole moment and a finite quadrupole moment that is concordant with that of Tyr. Accordingly, substitution of the Tyr residues within the PLD of FUS with Phe residues causes a diminution of the driving forces for phase separation, measured again in terms of increased values for  $c_{\text{sat}}$ . The roles of hydrophobic stickers have been made clear in the work of Riback et al. (139), who quantified the effects of titrating hydrophobic residues on the driving forces for collapse and phase separation of the polyA RNA binding protein PAB1.

Recent work of Castañeda and coworkers (41, 181) has shown the validity of the distinctions between stickers and spacers for explaining the impact of amyotrophic lateral sclerosis-related mutations within the protein UBQLN2 on its phase behavior. Mutations to stickers alter the driving forces for phase separation, whereas mutations to spacer residues contribute to changes in molecular dynamics as measured by the recovery of fluorescence after photobleaching. Interestingly, mutations to spacer residues have minimal effects on the driving forces for phase separation, a result that is concordant with the observations of Wang et al. (170), who found that changes to the PLD and RBD of FUS that lie outside of the identified stickers (Tyr and Arg) impact the material properties of condensates without altering the driving forces for phase separation.

The impact of charged residues as stickers was explored in the DEAD box helicase protein DDX4, which drives the formation of nuage bodies. Nott et al. (121) were the first to show the importance of clusters of positively and negatively charged residues along the linear sequence, with modest sequence changes that disrupt these charged stickers preventing phase separation in cells through a reduction in valence without changing sequence composition. They were also the first to identify the importance of complementary interactions between cationic and Phe (aromatic) residues as drivers of phase separation. The importance of linear clustering of charged stickers was also uncovered by Pak et al. (123), who quantified the phase behavior of a de novo designed IDR, the nephrin intracellular domain (NICD), in cells and in vitro, showing that increased linear

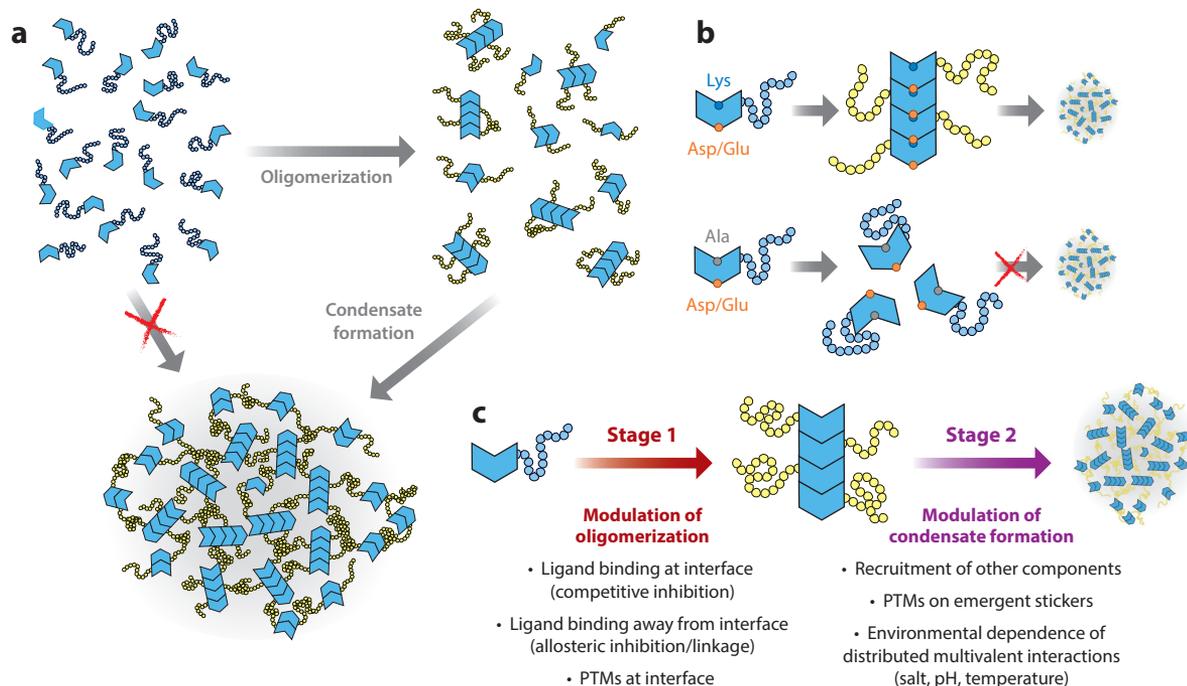
clustering of acidic residues within NICD enhances the driving forces for phase separation and the extent of physical crosslinking aided by cationic complexing polyions. As for RNA molecules, mutagenesis studies, design experiments, and coarse-grained simulations have demonstrated that purines are stronger stickers than pyrimidines, a result attributed to their double ring structure, which gives rise to a stronger aromatic system (22).

## EMERGENT VERSUS INTRINSIC STICKERS

Instantiations of the stickers-and-spacers model summarized above have focused on sequence-encoded features that dictate the apparent and effective valence of stickers. These stickers are intrinsic to the molecular architecture and are directly encoded into the sequence. Thus, we refer to these as intrinsic stickers. Recently, it has become clear that hierarchical assembly processes can give rise to emergent stickers, in which oligomerization and clustering or even microphase separation (141) can give rise to a de novo multivalent macromolecule that is itself able to drive the formation of condensates via the types of interactions that are proposed to apply for associative polymers (**Figure 5a**). Clusters that serve as generators of emergent stickers can form at a relatively low molecular concentration compared with the saturation concentration associated with their constitutive monomeric components. Importantly, from a theoretical standpoint, it can be argued that the interactions that drive oligomerization and clustering are likely to be distinct from the interactions that drive coalescence of oligomers into condensates, the conversion of clusters into crystals (165), or the transformation of oligomers into fibrils (131, 148).

We highlight several concrete examples that anchor the idea of emergent stickers being generated from oligomers or clusters. A subset of auxin response transcription factors (ARFs) in *Arabidopsis thaliana* undergo oligomerization driven by a folded C-terminal, PB1 (132). These linear oligomers lead to the formation of higher-order species, which themselves drive the formation of condensates through an IDR-dependent assembly process. In this system, oligomerized ARFs are in effect large multivalent biopolymers that drive condensate formation through the crosslinking of stickers in IDRs, whose multivalence is governed by the extent of oligomerization. If PB1 oligomerization is abrogated through a single lysine-to-alanine mutation, then higher-order oligomers and, consequently, condensates are unable to form (**Figure 5b**). As a second example, in the NPM1 pentamer, an emergent molecular species undergoes phase separation, as opposed to NPM1 monomers individually (108–111). A third example is the SPOP system, which has been explored in a series of elegant experiments (25, 101, 129). Finally, dimerization of HP1 $\alpha$ / $\alpha$  plays a key role in forming a species with the requisite multivalence to undergo phase separation (84, 159). A synthetic system where oligomerization controls the valence of IDRs that drive condensate formation is the Corelet system designed by Bracha et al. (26). In this case, the valence of IDRs appended to the oligomeric ferritin core is controlled by light, and the driving forces for phase separation, as quantified by full coexistence curves measured in living cells, are governed by the valence of the IDRs. In all of these systems, oligomerization that leads to emergent multivalence of stickers involves either evolved or designed interactions that are clearly orthogonal to the interactions that drive condensate formation through multivalence of stickers in IDRs.

A simple rationalization for the benefit of oligomerization and clustering is that they help to prepay some of the entropic penalty, a feature that can only be truly realized if the modes of interaction that drive oligomerization and subsequent condensate formation are distinct. This condition is well aligned with the observation that many of the proteins that undergo phase separation possess a modular architecture with distinct interaction domains (both IDRs and folded binding domains). The existence of orthogonal modes of intermolecular interaction allows the driving force for assembly to be tuned at (at least) two independent and complementary sites (**Figure 5c**).



**Figure 5**

General model for emergent stickers formed through oligomerization, linear polymerization, and/or clustering. (a) Depiction of monomers of ARF19 (*solid shapes*) that correspond to the PB1 domain and the disordered low-complexity prion-like domain shown as a string of smaller blue spheres tethered to the PB1 domain. Monomers lack the requisite valence to drive condensate formation, but oligomerization gives rise to polymers with emergent multivalence of IDRs (*yellow*). Polymers of ARF19 can drive condensate formation through physical crosslinking among IDRs. (b) ARF19 molecules undergo spontaneous polymerization through electrostatic interactions that are mediated via complementary interfaces involving the PB1 domain. Neutralization of a lysine residue abrogates polymerization and this in turn prevents condensate formation. (c) Schematic that summarizes the modus operandi for condensate formation through crosslinks among emergent stickers that result from oligomerization, polymerization, and/or cluster formation. For a system that gives rise to emergent stickers, condensate formation can be regulated at two levels: In stage 1, an effectively binary regulation that dictates whether oligomerization occurs (modulation of valence), and in stage 2, a second level in which the strength of emergent stickers can be altered. Note that, temporally, the order in which these levels of modulation occur is irrelevant. As a tangible example, in a scenario in which IDR phosphorylation weakens the strength of emergent stickers, the act of phosphorylation could happen before or after oligomerization. The binding of ligands, which could include other proteins, nucleic acids, or small molecules, either may lead to a conformational transition that allows homotypic oligomerization or could itself drive heterotypic assembly. In principle, multiple nested layers of assembly via orthogonal interaction modes provide the foundations for arbitrarily complex regulation. Abbreviations: IDR, intrinsically disordered region; PTM, post-translational modification.

From a regulatory standpoint, this allows one set of regulatory systems to control on–off interactions (e.g., inhibition or promotion of oligomerization or clustering) and another to tune the molecular details of the condensate by modulating the strength of emergent stickers. While we describe oligomerization in this review in terms of a conventional and stoichiometric biochemical phenomenon (i.e., dimerization, polymerization, etc.), oligomerization could also itself be driven by weak multivalent interactions, which would necessarily be chemically orthogonal to those that drive higher-order assembly. The multiresolution nature of the stickers-and-spacers model is appealing, as the emergence of new stickers is well described as a fractal (self-similar) phenomenon, allowing the same theoretical framework to be quantitatively applied irrespective of the molecular nature and length scale.

## CONCLUDING REMARKS

The field of intracellular phase transitions is evolving rapidly as we learn more about the molecular drivers of biomolecular condensates and the contributions of condensates to specific biological functions. Condensates appear to be ubiquitous within cells, and novel cellular functions are being ascribed to newly discovered condensates. Accounts of these novel functions and details about the molecular drivers of condensates are emerging at a frenetic pace. In this review, we focus on a specific physical framework, namely, the stickers-and-spacers model, adapted from the field of associative polymers, to describe the molecular grammar that underlies the architecture, sequence-encoded driving forces, and evolution of the multivalent protein and RNA molecules that drive condensate formation. Mapping of the stickers-and-spacers framework to biomacromolecules is in its infancy. However, the validity of this framework is coming into sharp focus as more accounts emerge of its utility for explaining measured phase behavior and for predicting and designing phase behavior. The availability of computational tools is further advancing our ability to dissect the interplay between spontaneous and driven processes in regulating and determining the phase behavior of mixtures of associative polymers. At this juncture, the stickers-and-spacers formalism seems like an apt modernization of classical theories developed for homopolymers and is proving to be relevant for describing phase transitions of multivalent protein and RNA molecules. The findings summarized in this review pave the way for understanding how the synergies of sticker and spacer interactions might be affected or modulated in multicomponent systems, which mimic naturally occurring biomolecular condensates—an important topic that merits intense study.

Predictions based on the stickers-and-spacers framework apply to systems with one or two types of multivalent protein or RNA molecules in a solvent. However, biomolecular condensates encompass hundreds of distinct types of macromolecules. A key concept that has to be generalized is that of saturation concentrations, as what we have adapted thus far applies strictly to two-component systems comprising a polymer plus a solvent. A recent computational study based on the LASSI simulation engine helps generalize the concept of saturation concentration by showing how obligate heterotypic interactions can give rise to apparent saturation concentrations that depend on the slopes of tie lines in multidimensional phase diagrams (35). The simulations, which are built on the stickers-and-spacers formalism, when combined with suitable experiments (140), should enable a rigorous mapping between the numbers of distinct components and the apparent saturation concentrations for each of the components. In fact, our generalizations of  $c_{\text{perc}}$  (see Equation 15) for an arbitrary number of stickers, as well as the findings reported by Choi et al. (35) based on the LASSI engine and by Riback et al. (140) based on experiments, help set the stage for connecting generalized observations from simulations of multicomponent systems to theories wherein each protein or RNA component has its own set of distinct stickers that may or may not interact with stickers on other protein or RNA molecules.

## DISCLOSURE STATEMENT

R.V.P. is a member of the Scientific Advisory Board of Dewpoint Therapeutics, Inc. This membership has not influenced the scientific content of this review. The other authors are not aware of any affiliations, memberships, funding, or financial holdings that might be perceived as affecting the objectivity of this review.

## ACKNOWLEDGMENTS

The US National Science Foundation (MCB-1614766), the US National Institutes of Health (5R01NS056114 and 1R01NS089932), the Human Frontier Science Program (RGP0034/2017),

and the St. Jude Research Collaborative on Membraneless Organelles fund ongoing efforts in the Pappu lab. J.-M.C. is currently funded by the Basic Science Research Program (2019R1A6A1A10073887) from the Ministry of Education of the Republic of Korea through the National Research Foundation of Korea. We are grateful to Simon Alberti, Priya Banerjee, Clifford Brangwynne, Carlos Castañeda, Hue-Sun Chan, Furqan Dar, Julie Forman-Kay, Titus Franzmann, Amy Gladfelter, Tyler Harmon, Anthony Hyman, Frank Jülicher, Richard Kriwacki, Erik Martin, Tanja Mittag, Ammon Posey, Michael Rosen, Lucia Strader, Andrea Soranno, and J. Paul Taylor for numerous stimulating discussions. We dedicate this review to the memory of Suzanne Eaton, a senior group leader at the Max Planck Institute for Cell Biology (MPI-CBG) and Genetics in Dresden, where the application of the stickers-and-spacers formalism matured through interactions with colleagues at the MPI. Suzanne was an inspiring scientist and human being, and her legacy will continue to live on through the efforts of scientists at the MPI-CBG and the community that stretches beyond.

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# Contents

The Physics of Cellular Decision Making During Epithelial–Mesenchymal Transition <i>Sbubham Tripathi, Herbert Levine, and Mobit Kumar Jolly</i> .....	1
Principles and Applications of Biological Membrane Organization <i>Wade F. Zeno, Kasey J. Day, Vernita D. Gordon, and Jeanne C. Stachowiak</i> .....	19
Mitochondria-Associated Proteostasis <i>Linhao Ruan, Yubao Wang, Xi Zhang, Alexis Tomaszewski, Joshua T. McNamara, and Rong Li</i> .....	41
Milestoning: An Efficient Approach for Atomically Detailed Simulations of Kinetics in Biophysics <i>Ron Elber</i> .....	69
Enhanced Diffusion and Chemotaxis of Enzymes <i>Mudong Feng and Michael K. Gilson</i> .....	87
Physical Principles Underlying the Complex Biology of Intracellular Phase Transitions <i>Jeong-Mo Choi, Alex S. Holehouse, and Robit V. Pappu</i> .....	107
Multifunctional Chaperone and Quality Control Complexes in Adaptive Immunity <i>Simon Trowitzsch and Robert Tampé</i> .....	135
Temperature, Dynamics, and Enzyme-Catalyzed Reaction Rates <i>Vickery L. Arcus and Adrian J. Mulholland</i> .....	163
Predicting Evolution Using Regulatory Architecture <i>Philippe Nghe, Marjon G.J. de Vos, Enzo Kingma, Manjunatha Kogenaru, Frank J. Poelwijk, Liedewij Laan, and Sander J. Tans</i> .....	181
Gene Regulation in and out of Equilibrium <i>Felix Wong and Jeremy Gunawardena</i> .....	199

Nonequilibrium Thermodynamics in Cell Biology: Extending Equilibrium Formalism to Cover Living Systems <i>Xiaona Fang and Jin Wang</i> .....	227
RNA Droplets <i>Kevin Rhine, Velinda Vidaurre, and Sua Myong</i> .....	247
The Role of Conformational Dynamics and Allostery in Modulating Protein Evolution <i>Paul Campitelli, Tusbar Modi, Sudbir Kumar, and S. Banu Ozkan</i> .....	267
Light Microscopy of Mitochondria at the Nanoscale <i>Stefan Jakobs, Till Stephan, Peter Ilgen, and Christian Brüser</i> .....	289
Insights into the Structure, Function, and Dynamics of the Bacterial Cytokinetic FtsZ-Ring <i>Ryan McQuillen and Jie Xiao</i> .....	309

## Indexes

Cumulative Index of Contributing Authors, Volumes 45–49 .....	343
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## Errata

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